

Matrix Factorization

March 17, 2020

Data Science CSCI 1951A

Brown University

Instructor: Ellie Pavlick

HTAs: Josh Levin, Diane Mutako, Sol Zitter

Announcements

- ...

Today

- Matrix Factorization with SVD
- Applications to: Topic Modeling, Recommendation Systems

Use Cases

- Matrix Completion:
 - Recommendation—if someone likes/watches/clicks on this, they might also like/watch/click on that
- Dimensionality Reduction:
 - Embeddings/Denoising—Can I throw away features without losing performance? Can I throw away noisy features and actually increase performance?

What is dimensionality reduction?

Clicks	Recency	Reading Level	Photo	Title: "new"	Title: "tax"	Title: "this"	...
10	1.3	11	1	1	0	0	...
1000	1.7	3	1	0	0	1	...
1000000	2.4	2	1	0	0	1	...
1	5.9	19	0	0	0	0	...

What is dimensionality reduction?

Clicks	Recency	Reading Level	Photo	Title: "new"	Title: "tax"	Title: "this"	...
--------	---------	---------------	-------	--------------	--------------	---------------	-----

10	1.3	11	1	1	0	0	...
----	-----	----	---	---	---	---	-----

often 1000s or (100s of 1000s) of features

1000	1.7	3	1	0	0	1	...
------	-----	---	---	---	---	---	-----

1000000	2.4	2	1	0	0	1	...
---------	-----	---	---	---	---	---	-----

1	5.9	19	0	0	0	0	...
---	-----	----	---	---	---	---	-----

What is dimensionality reduction?

Clicks	Recency	Reading Level	Photo	Title: "new"	Title: "tax"	Title: "this"	...
--------	---------	---------------	-------	--------------	--------------	---------------	-----

10	1.3	11	1	1	0	0	...
----	-----	----	---	---	---	---	-----

many (most) are redundant or useless

1000	1.7	3	1	0	0	1	...
------	-----	---	---	---	---	---	-----

1000000	2.4	2	1	0	0	1	...
---------	-----	---	---	---	---	---	-----

1	5.9	19	0	0	0	0	...
---	-----	----	---	---	---	---	-----

What is dimensionality reduction?

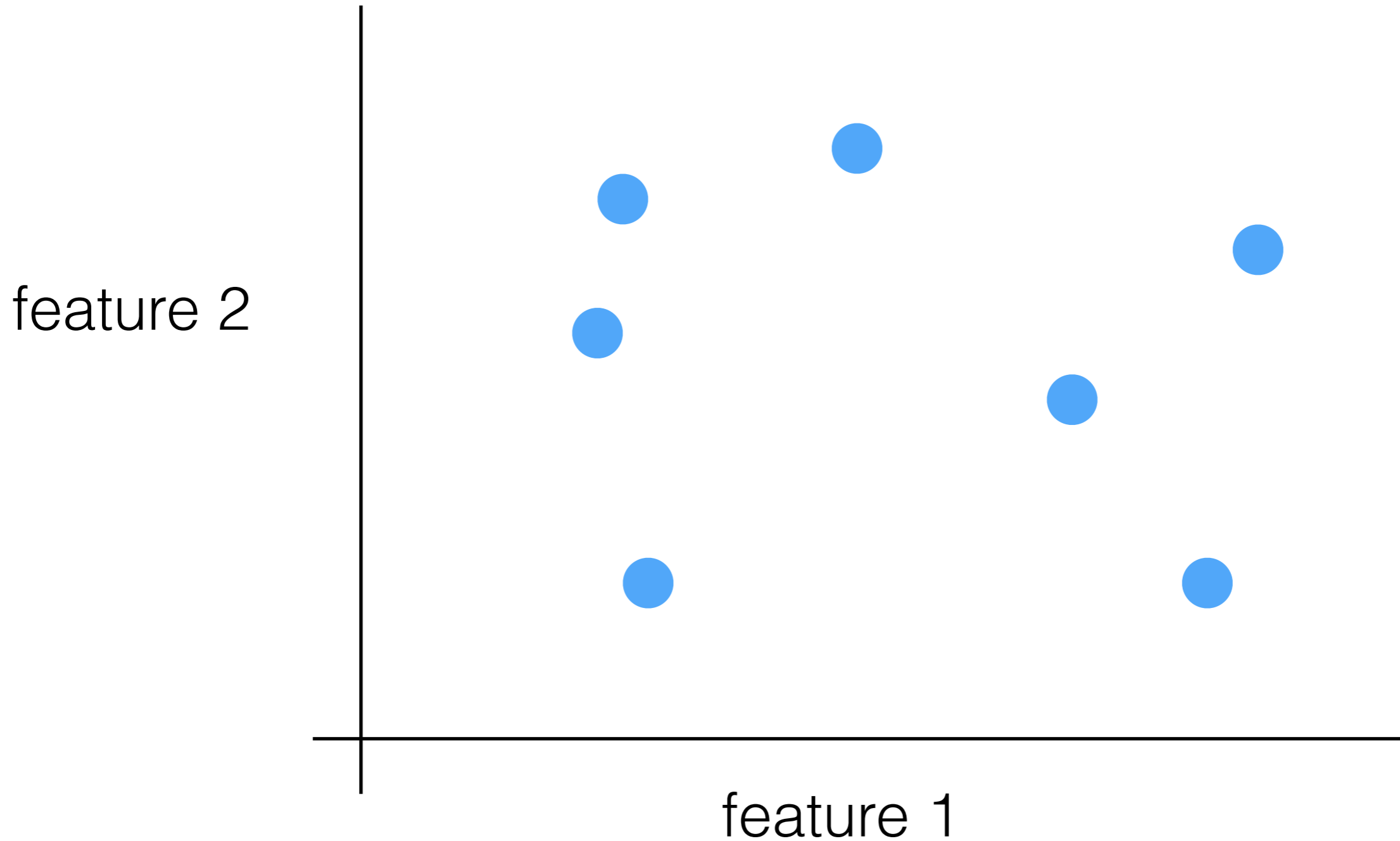
Clicks	Recency	Reading Level	Photo	Title: "new"	Title: "tax"	Title: "this"	...
10	1.3	11	1	1	0	0	...
1000	1.7	3	1	0	0	1	...
1000000	2.4	2	1	0	0	1	...
1	5.9	19	0	0	0	0	...

- slower to train

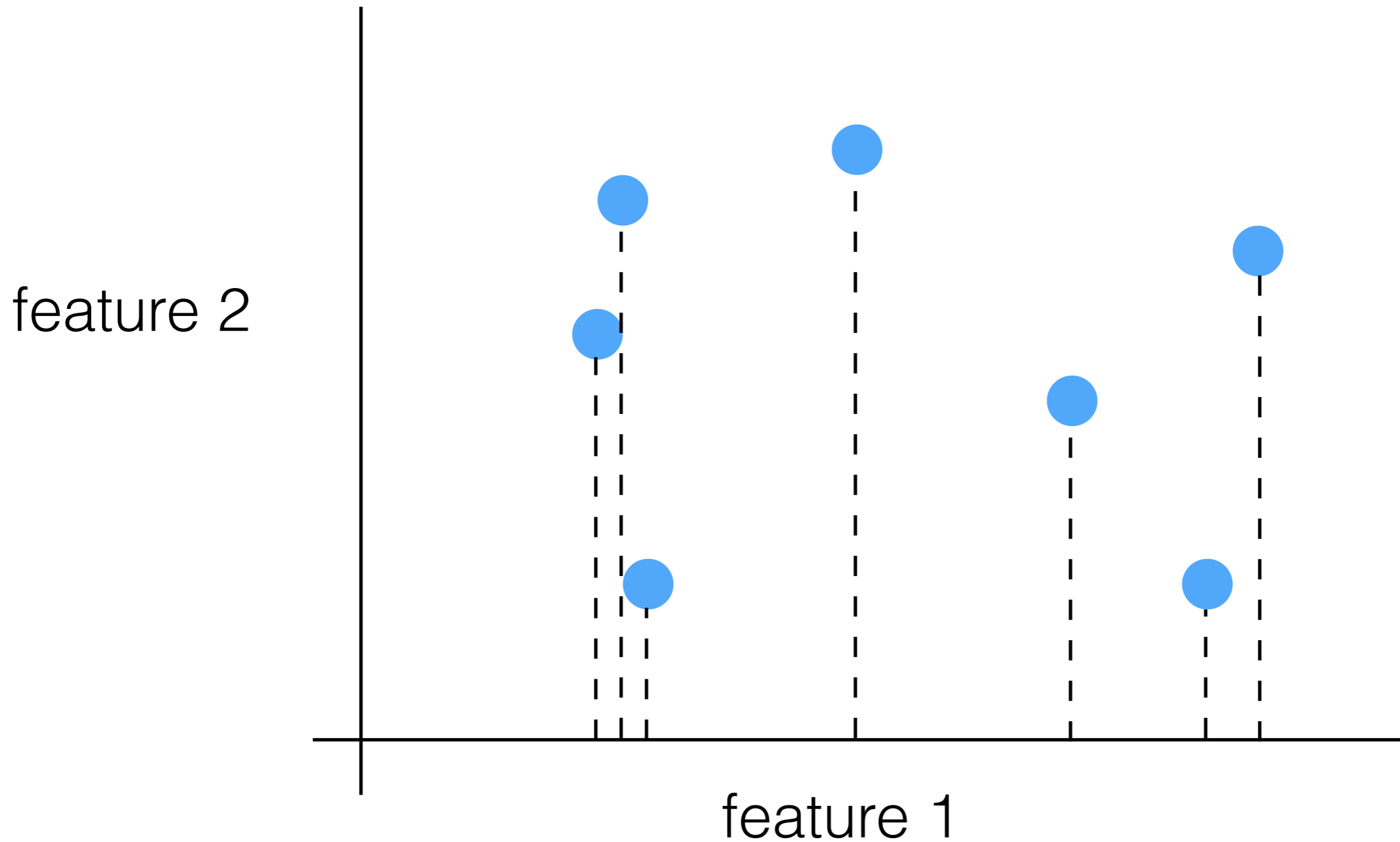
- easier to overfit

- harder to visualize/interpret ()*

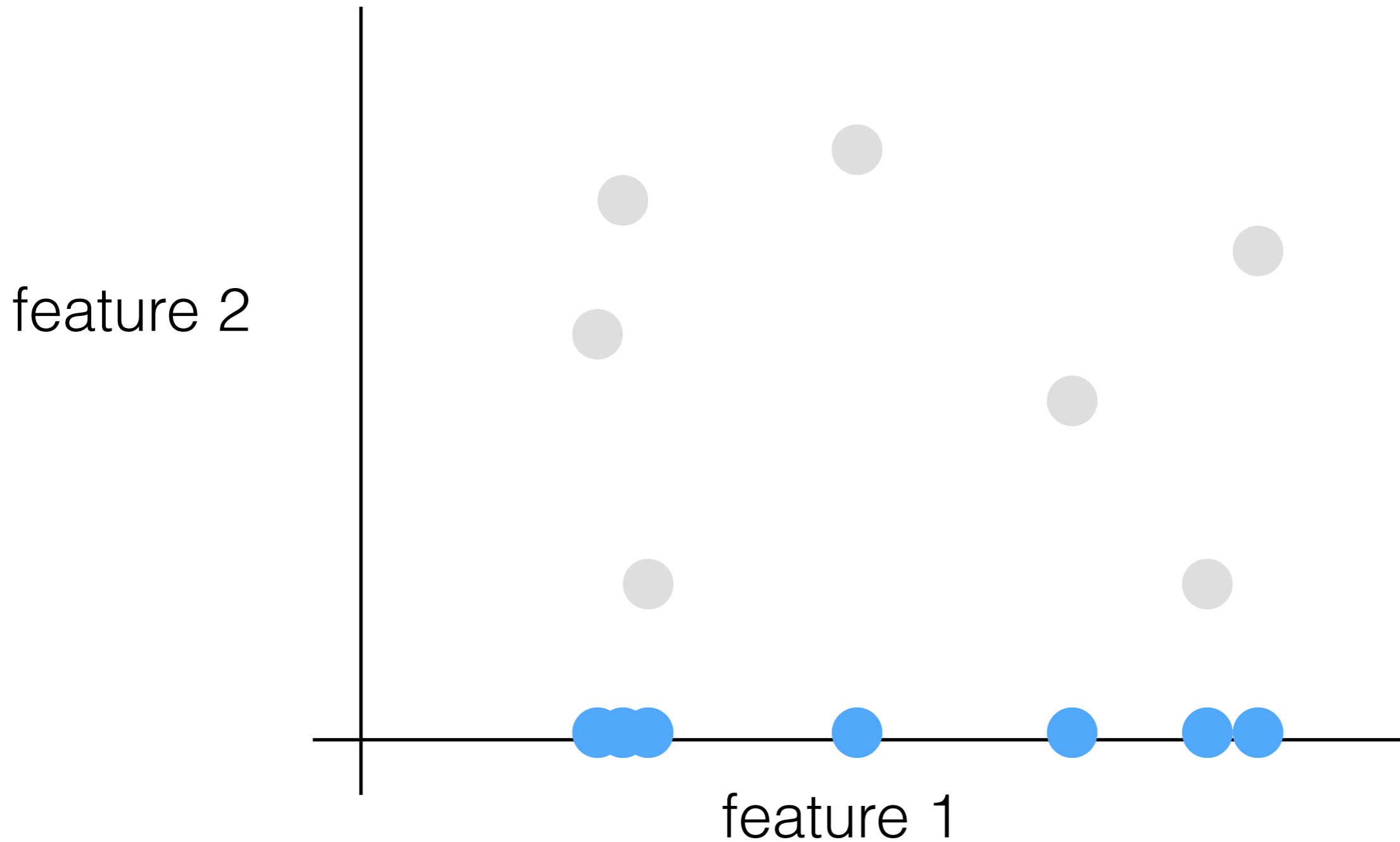
Principle Component Analysis (PCA)



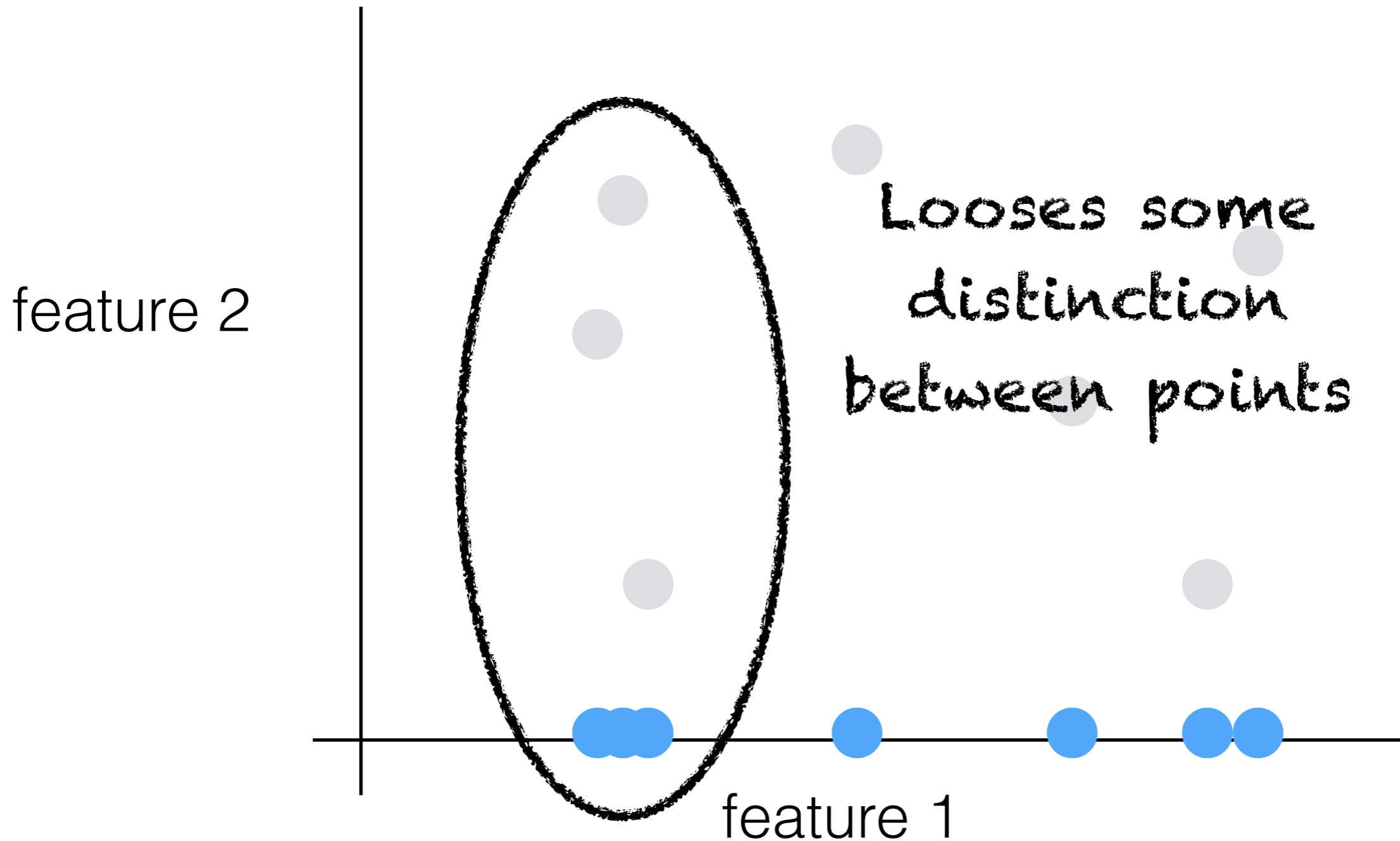
Principle Component Analysis (PCA)



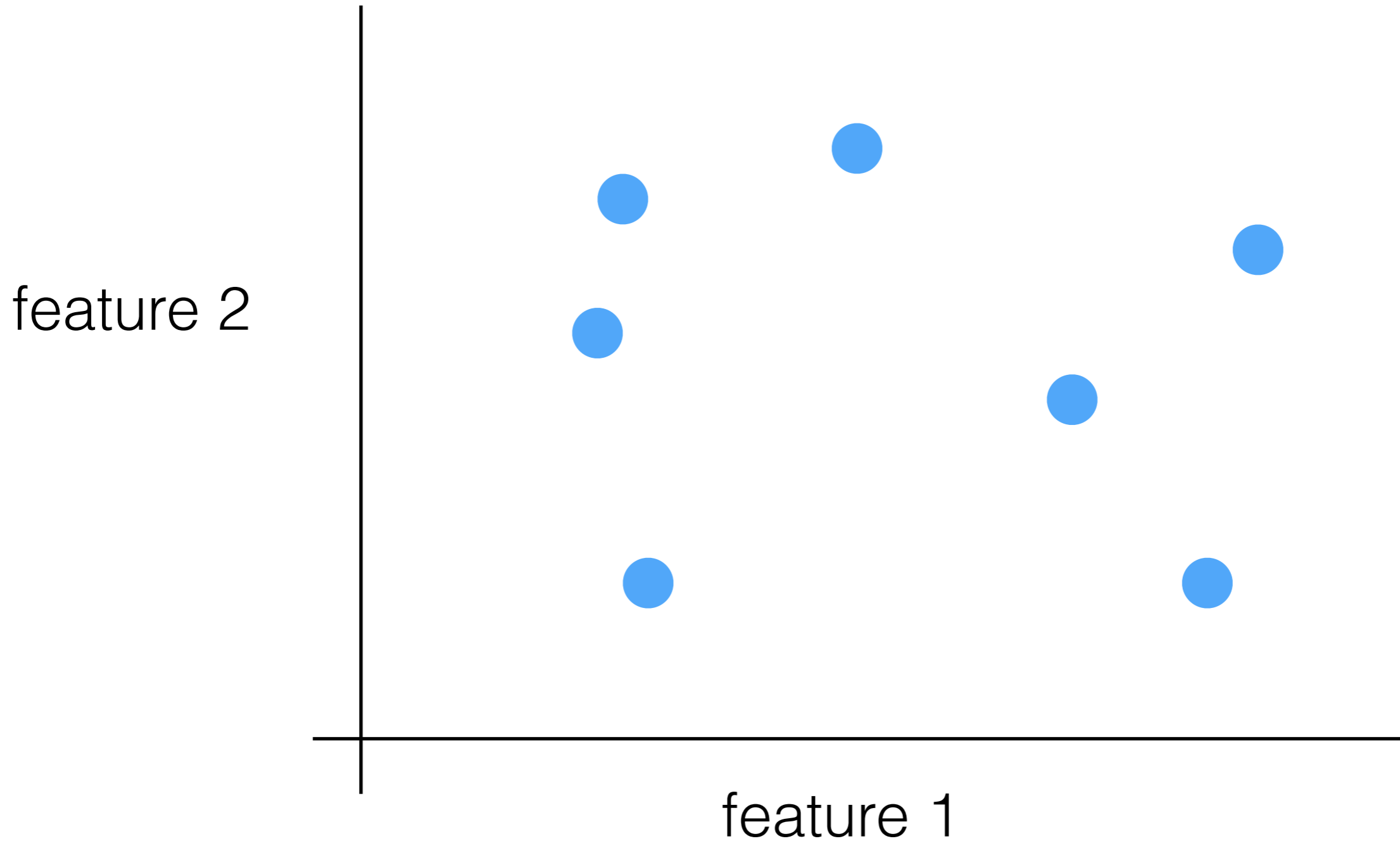
Principle Component Analysis (PCA)



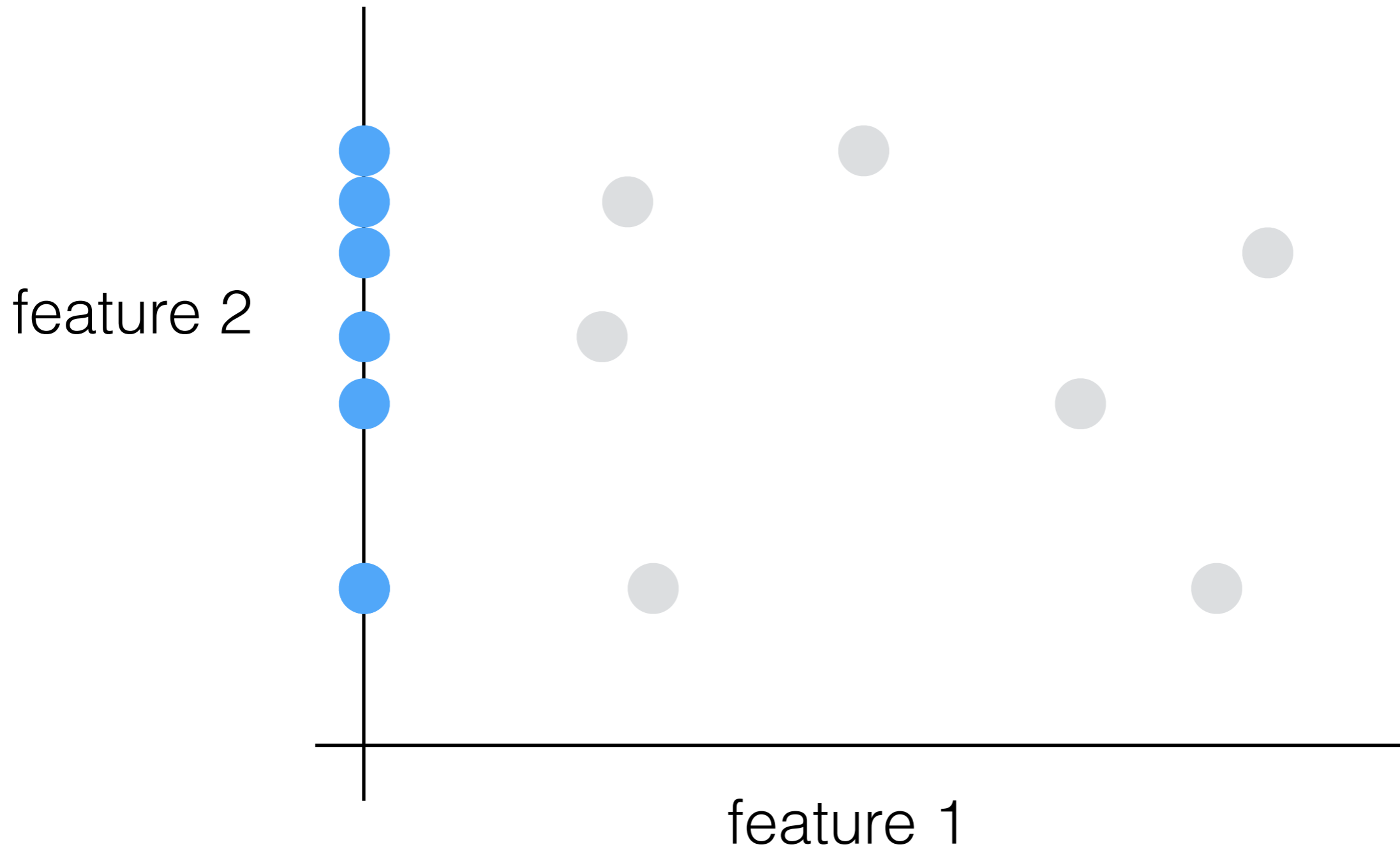
Principle Component Analysis (PCA)



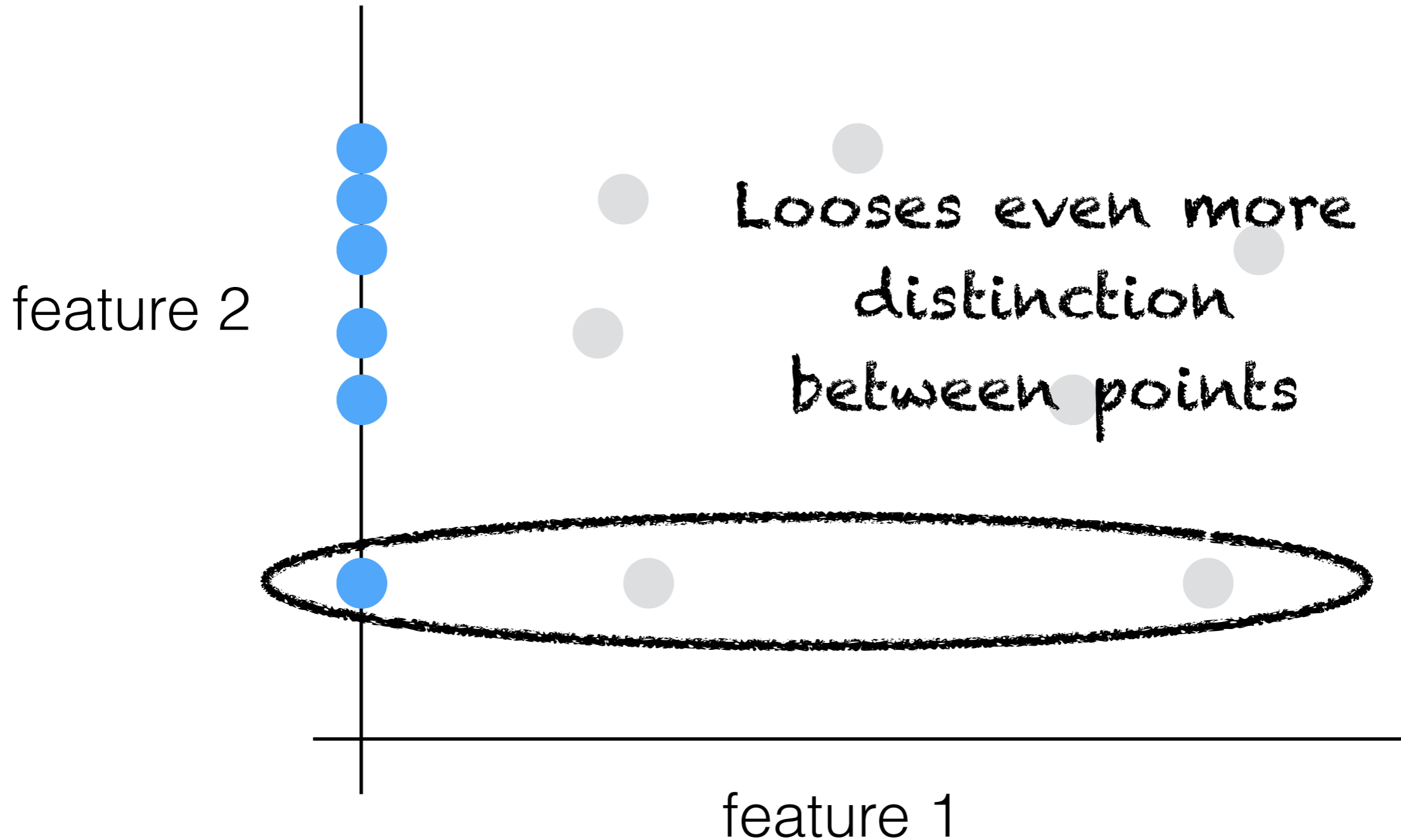
Principle Component Analysis (PCA)



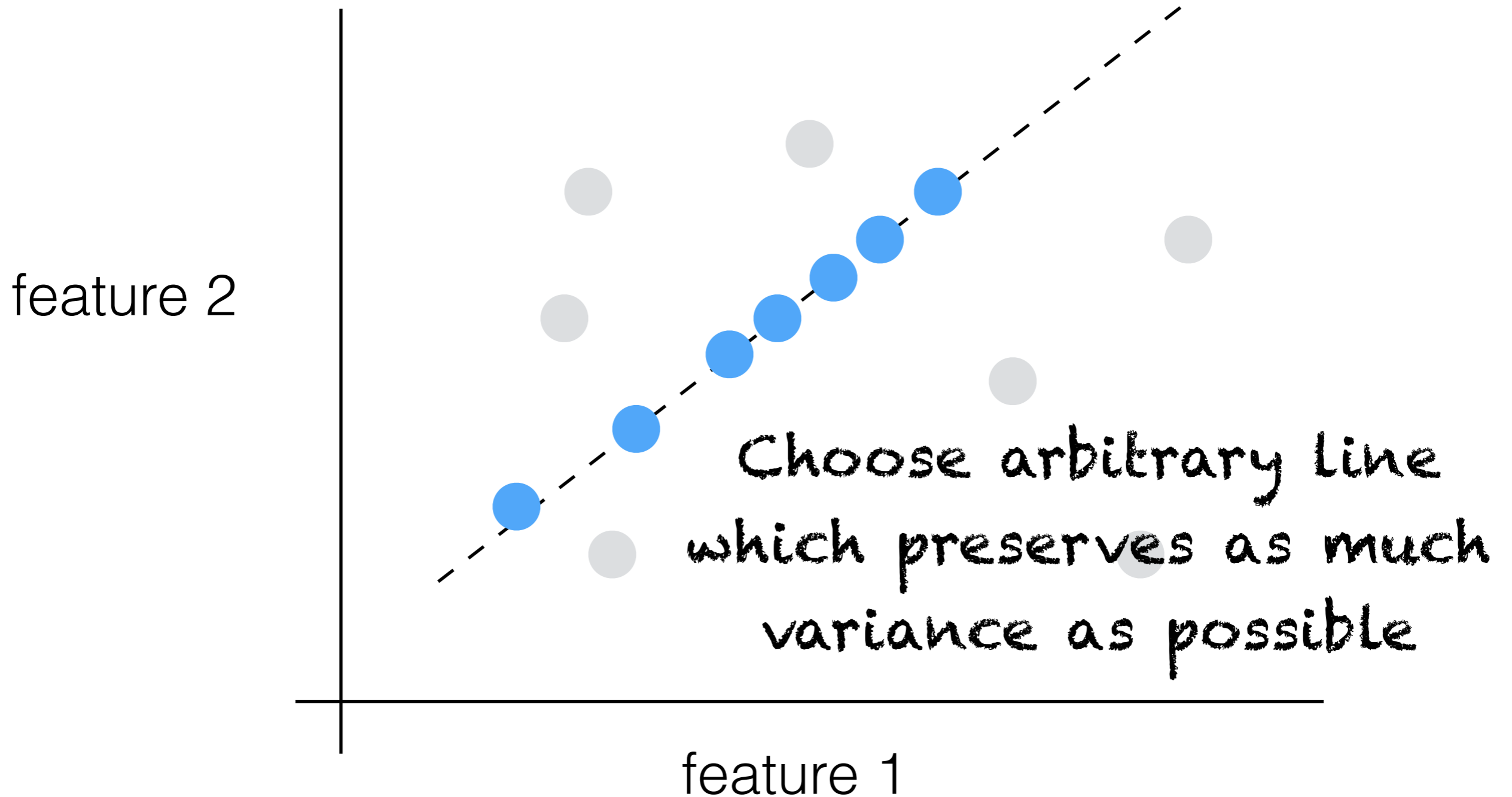
Principle Component Analysis (PCA)



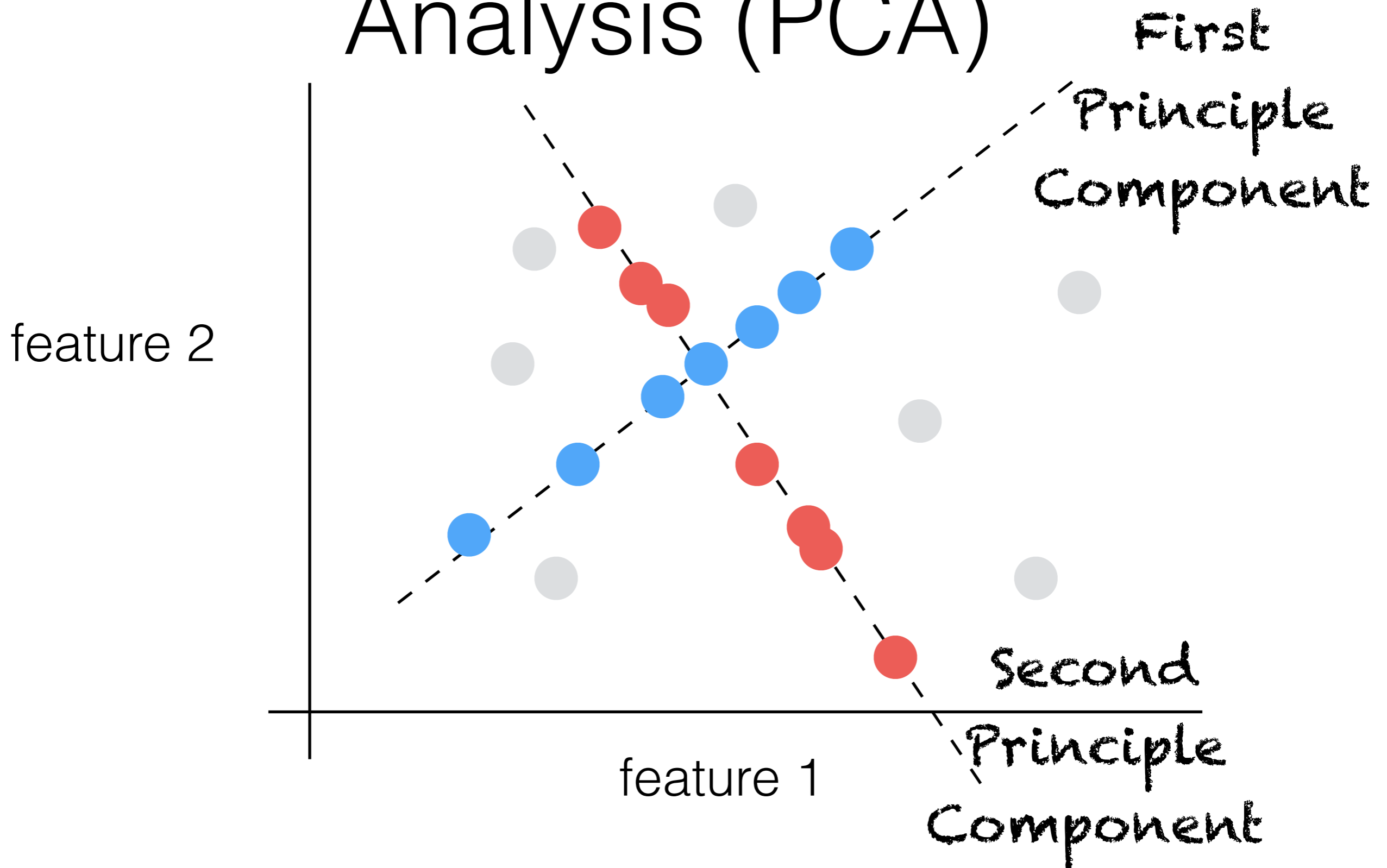
Principle Component Analysis (PCA)



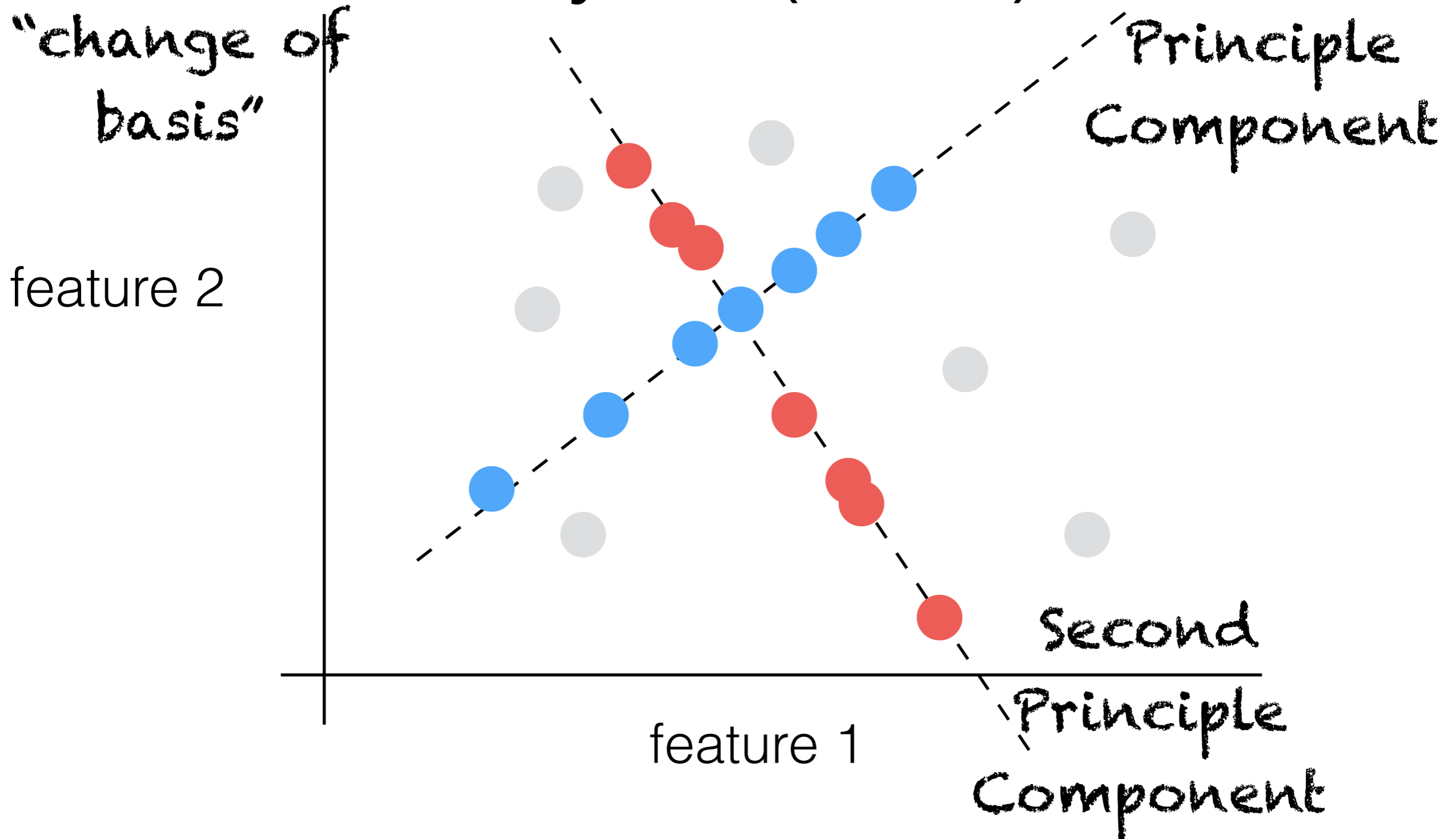
Principle Component Analysis (PCA)



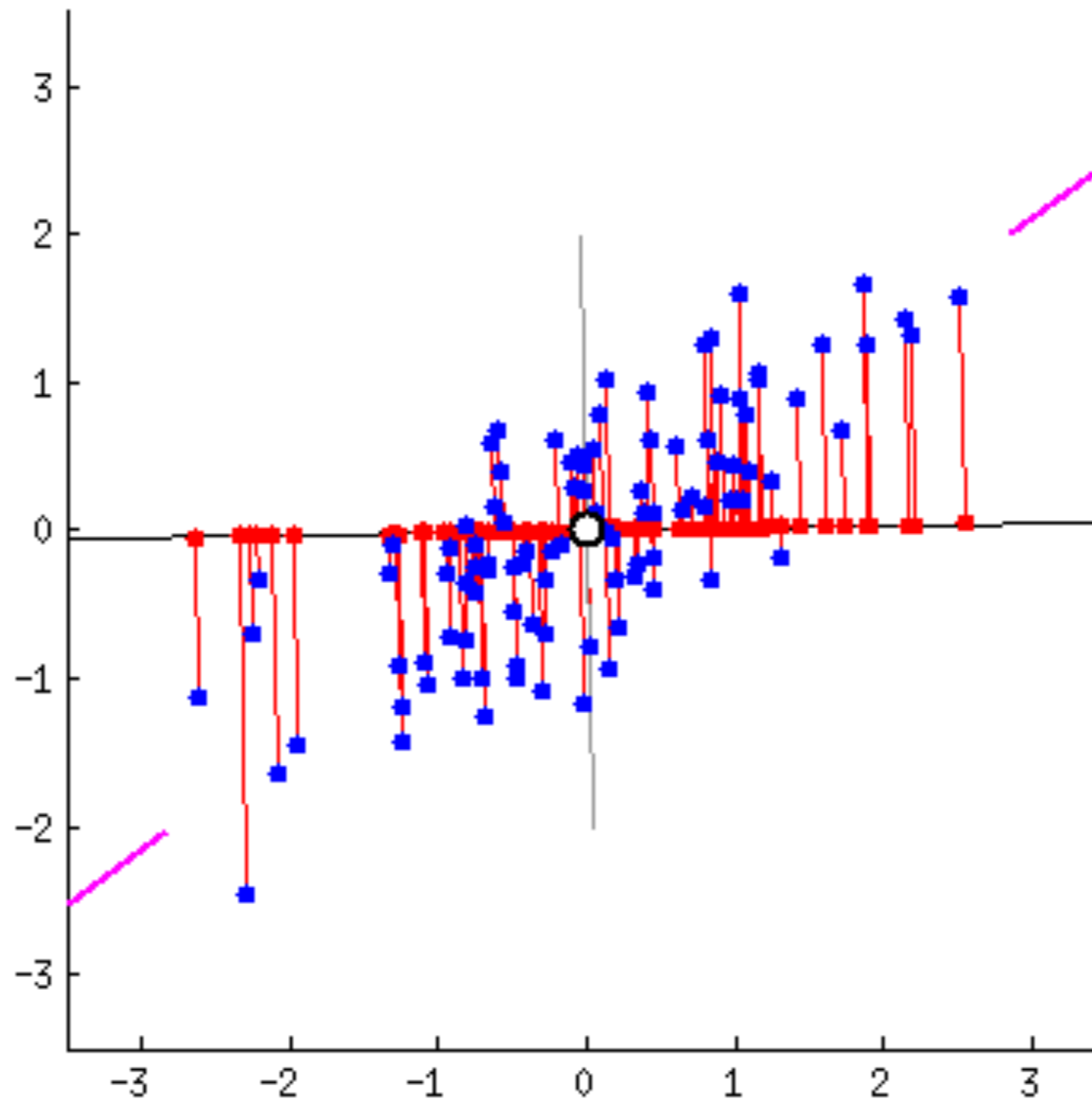
Principle Component Analysis (PCA)



Principle Component Analysis (PCA)



Principle Component Analysis (PCA)



Principle Component Analysis (PCA)

- Eigenvalue Decomposition of covariance matrix
- Singular Value Decomposition of the data matrix

Principle Component Analysis (PCA)

- Eigenvalue Decomposition of covariance matrix
- **Singular Value Decomposition of the data matrix**

Principle Component Analysis (PCA)

- Eigenvalue Decomposition of covariance matrix
- **Singular Value Decomposition of the data matrix**

Technically, PCA \neq SVD

Principle Component Analysis (PCA)

- Eigenvalue Decomposition of covariance matrix
- **Singular Value Decomposition of the data matrix**

Technically, PCA \neq SVD
(but in practice these are used interchangeably)

Rank of a matrix

2	1	1
4	3	1
2	0	2
8	4	4

Rank of a matrix

2	=	1	+	1
4	=	3	+	1
2	=	0	+	2
8	=	4	+	4

Rank of a matrix

2	=	1	+	1
4	=	3	+	1
2	=	0	+	2
8	=	4	+	4

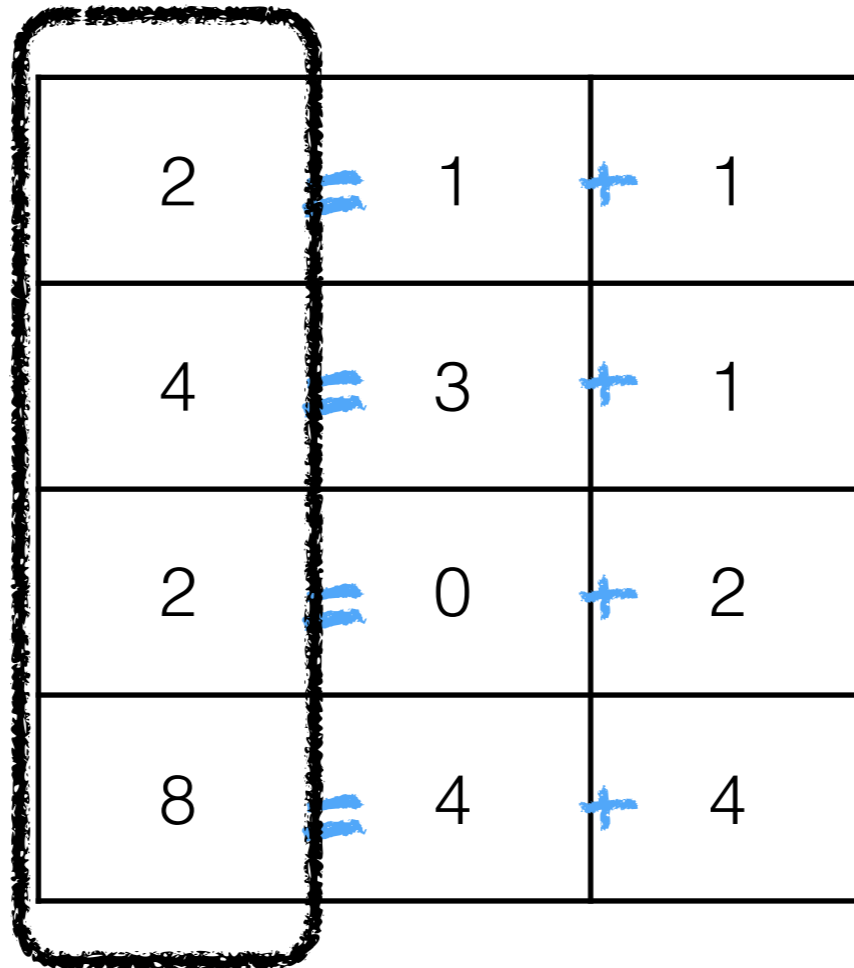
Rank = 2

Rank of a matrix

No new signal



2	=	1	+	1
4	=	3	+	1
2	=	0	+	2
8	=	4	+	4



Rank = 2

Clicker Question!

Clicker Question!

What is the rank of this matrix?

	the	congress	parliament	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

- a) 5
- b) 4
- c) 3
- d) 2
- e) 1

Clicker Question!

What is the rank of this matrix?

	the	congress	parliament	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

- a) **5**
- b) **4**
- c) **3**
- d) **2**
- e) **1**

Clicker Question!

What is the rank of this matrix?

	the		parliament	US	UK
doc1	1		1	1	0
doc2	1		1	0	1
doc3	1		0	1	0
doc4	1		1	0	1

- a) 5
- b) 4
- c) 3
- d) 2
- e) 1

Clicker Question!

What is the rank of this matrix?

	the		parliament	US	UK
doc1	1		1	1	0
doc2	1		1	0	1
doc3	1		0	1	0
doc4	1		1	0	1

- a) **5**
- b) **4**
- c) **3**
- d) **2**
- e) **1**

Clicker Question!

What is the rank of this matrix?

			parliament	US	UK
doc1			1	1	0
doc2			1	0	1
doc3			0	1	0
doc4			1	0	1

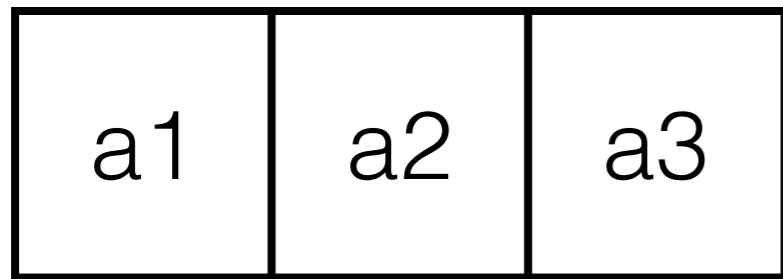
- a) 5
- b) 4
- c) 3
- d) 2
- e) 1

Rank of a matrix

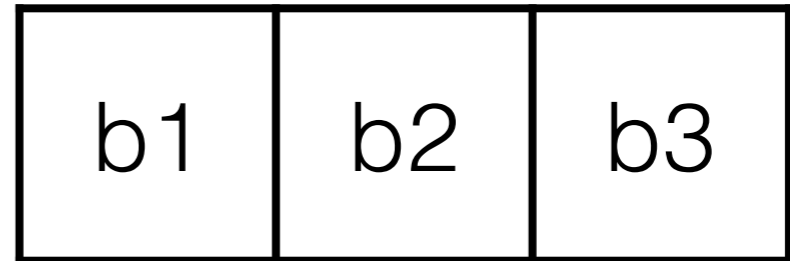
	the	congress	parliament	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

“Low Rank Assumption”: we typically assume that our features contain a large amount of redundant information

Matrix Arithmetic Refresh

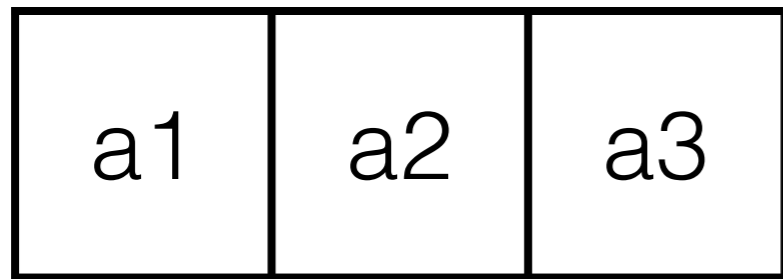


\rightarrow
a

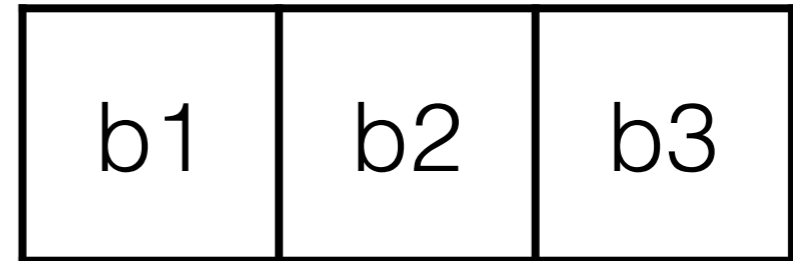


\rightarrow
b

Matrix Arithmetic Refresh



\vec{a}



\vec{b}

$$\vec{a} \cdot \vec{b} = (a1 \times b1) + (a2 \times b2) + (a3 \times b3)$$

Matrix Arithmetic Refresh

a11	a12	a13
a21	a22	a23
a31	a32	a33

A

b11	b12
b21	b22
b31	b32

B

Matrix Arithmetic Refresh

a11	a12	a13
a21	a22	a23
a31	a32	a33

A
3x3

b11	b12
b21	b22
b31	b32

B
3x2

Matrix Arithmetic Refresh

a11	a12	a13
a21	a22	a23
a31	a32	a33

A
3x3

b11	b12
b21	b22
b31	b32

B
3x2

Matrix Arithmetic Refresh

a11	a12	a13
a21	a22	a23
a31	a32	a33

A
3x3

b11	b12
b21	b22
b31	b32

B
3x2

??	??
??	??
??	??

AB
3x2

Matrix Arithmetic Refresh

a11	a12	a13
a21	a22	a23
a31	a32	a33

A

$m \times k$

b11	b12
b21	b22
b31	b32

B

$k \times n$

??	??
??	??
??	??

AB

$m \times n$

Matrix Arithmetic Refresh

\vec{a}_1
\vec{a}_2
\vec{a}_3

A

\vec{b}_1	\vec{b}_2
-------------	-------------

B

$a_1 \cdot b_1$	$a_2 \cdot b_1$
$a_2 \cdot b_1$	$a_2 \cdot b_2$
$a_3 \cdot b_1$	$a_3 \cdot b_2$

AB

Matrix Arithmetic Refresh

\vec{a}_1
\vec{a}_2
\vec{a}_3

A

\vec{b}_1	\vec{b}_2
-------------	-------------

B

$a_1 \cdot b_1$	$a_2 \cdot b_1$
$a_2 \cdot b_1$	$a_2 \cdot b_2$
$a_3 \cdot b_1$	$a_3 \cdot b_2$

AB

$$AB[i][j] = a_i \cdot b_j$$

Clicker Question!

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

(a)

13	25
13	6

(b)

14	7	6
20	10	10
26	13	14

(c)

13	11
25	25

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

(a)

13	25
13	6

(b)

14	7	6
20	10	10
26	13	14

(c)

13	11
25	25

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

(1×2)
+
 (2×1)
+
 (3×3)

(a)

13	25
13	6

(b)

14	7	6
20	10	10
26	13	14

(c)

13	11
25	25

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

2
+
2
+
9

(a)

13	25
13	6

(b)

14	7	6
20	10	10
26	13	14

(c)

13	11
25	25

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

4
+
4
+
3

(a)

13	25
13	6

(b)

14	7	6
20	10	10
26	13	14

(c)

13	11
25	25

Clicker Question!

1	2	3
3	4	5

X

2	4
1	2
3	1

(a)

13	25
13	6

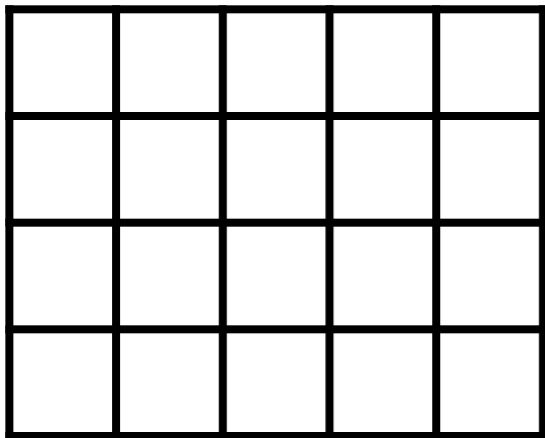
(b)

14	7	6
20	10	10
26	13	14

(c)

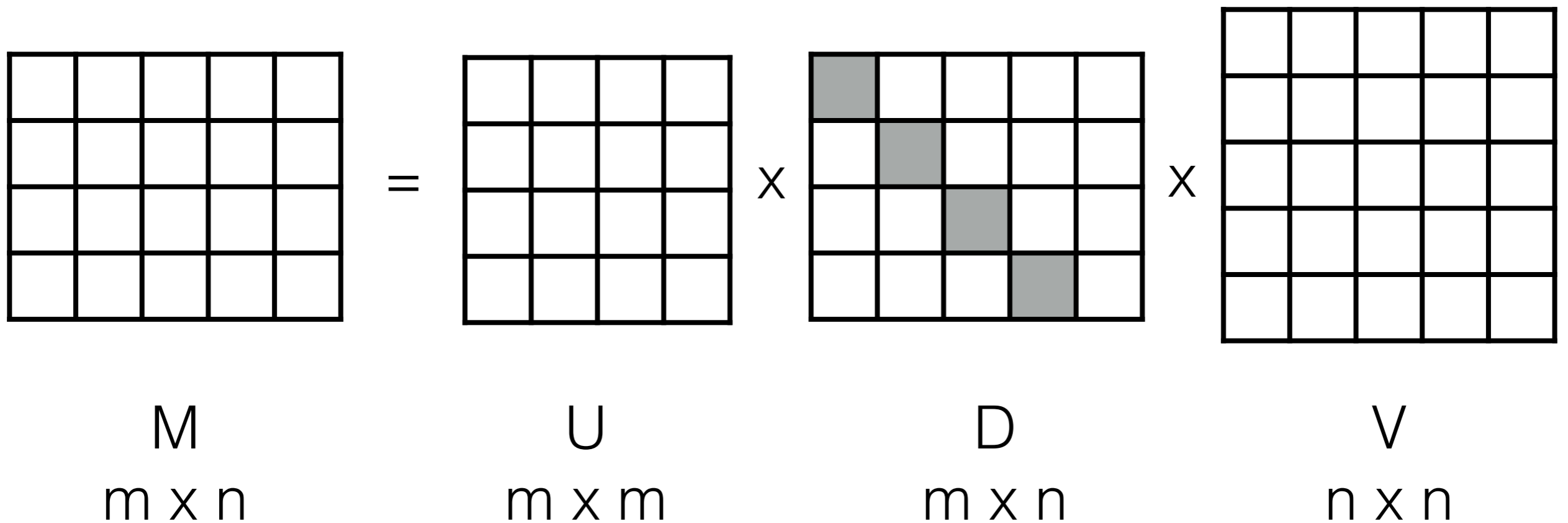
13	11
25	25

Singular Value Decomposition (SVD)

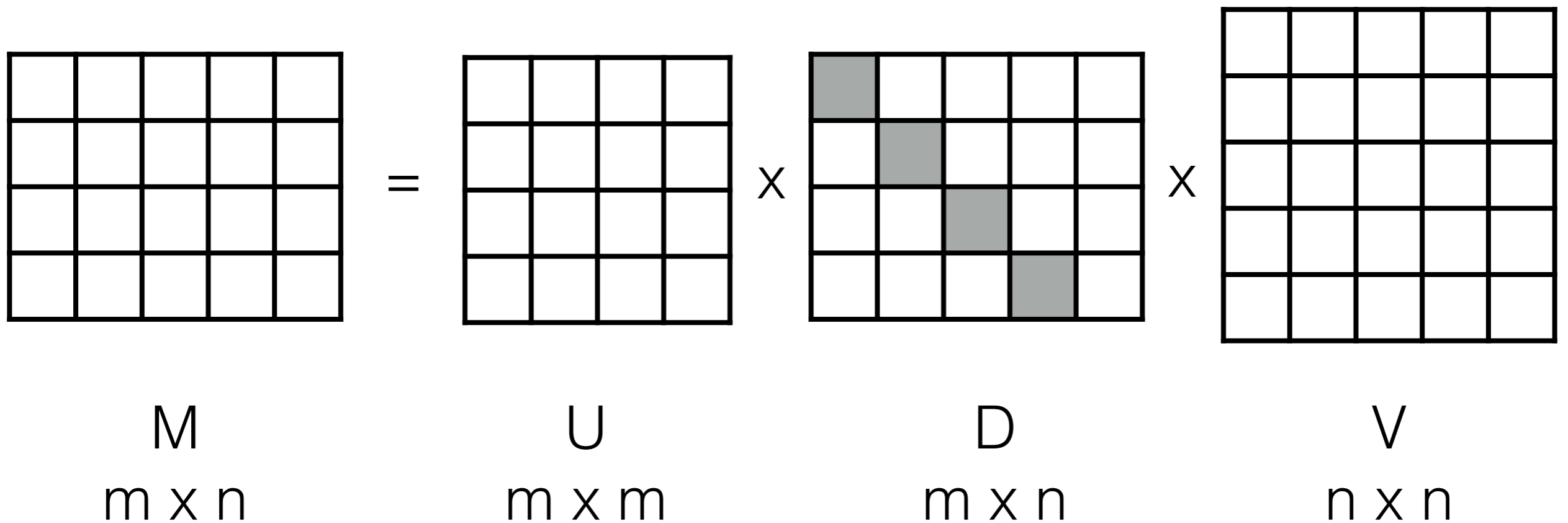


M
m x n

Singular Value Decomposition (SVD)

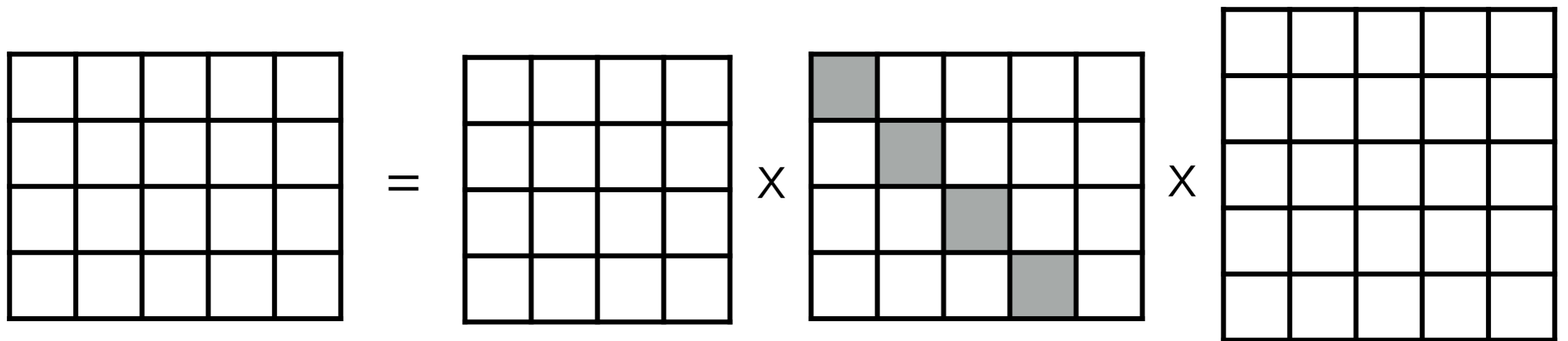


Singular Value Decomposition (SVD)



Data Matrix

Singular Value Decomposition (SVD)



M
 $m \times n$

U
 $m \times m$

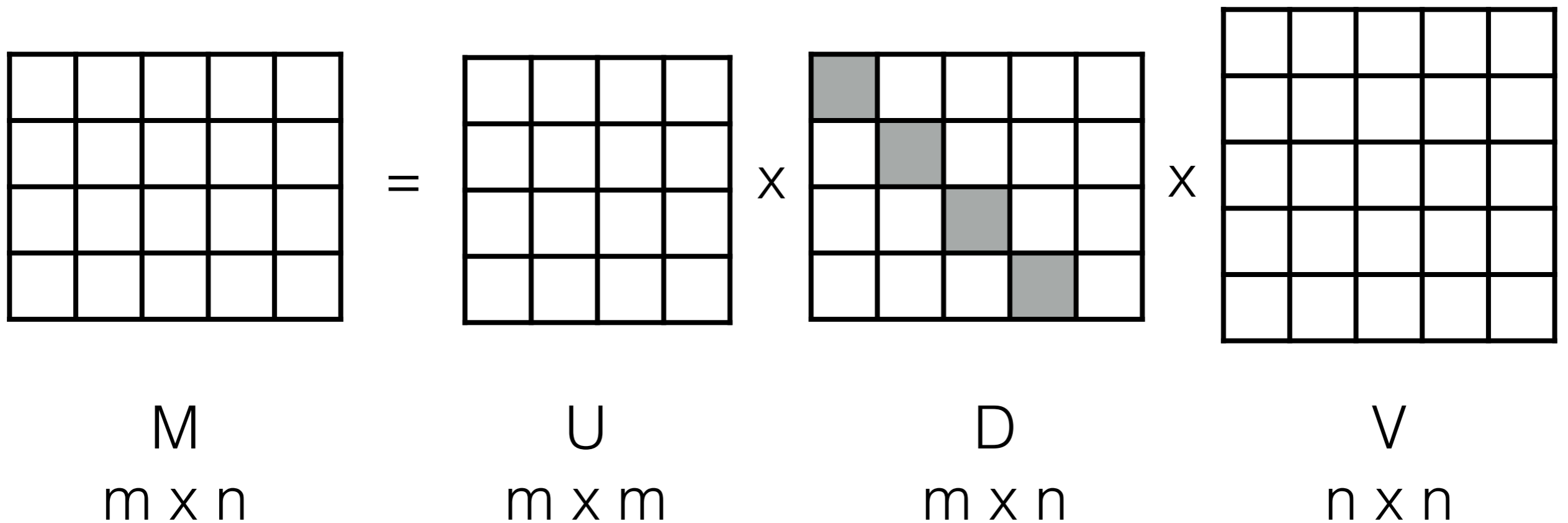
D
 $m \times n$

V
 $n \times n$

Data Matrix

*Singular
Values of M*

Singular Value Decomposition (SVD)

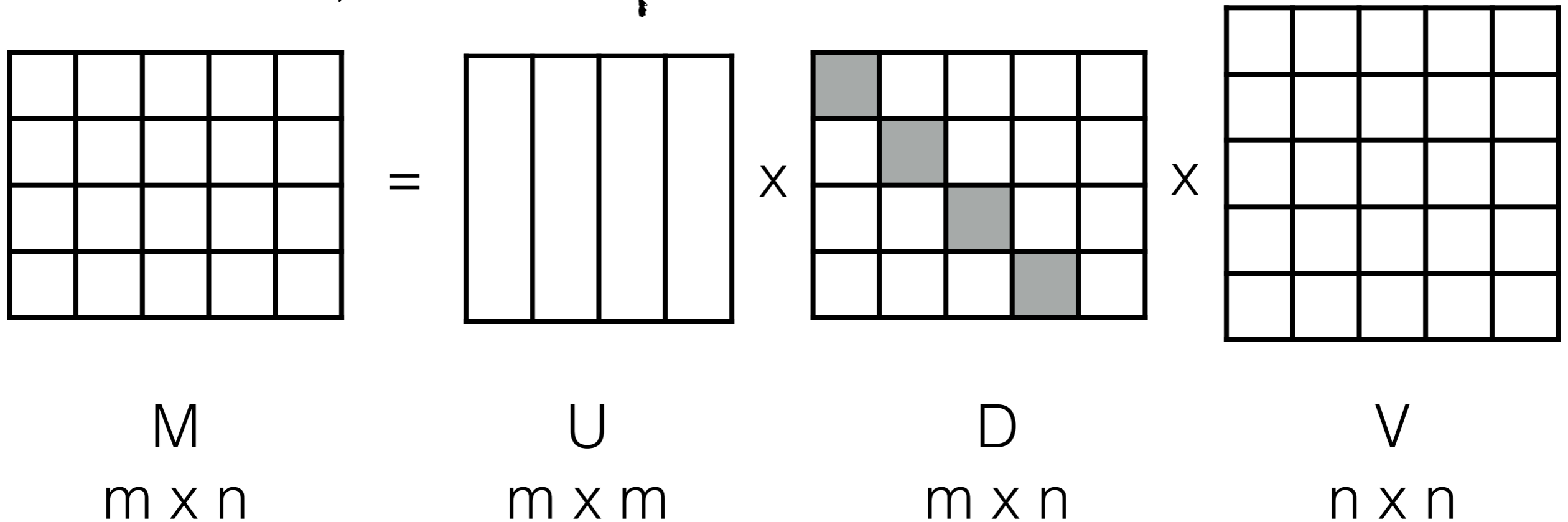


Data Matrix

Singular
Values of M
(#non-zero = rank M)

Singular Value

Representation of rows of M in new feature space on (SVD)



Data Matrix

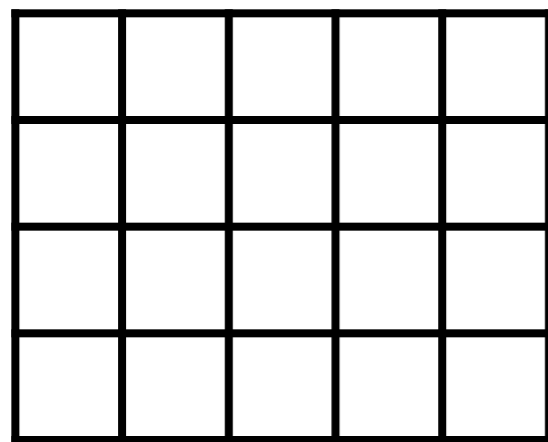
Singular
Values of M
(#non-zero = rank M)

Singular Value

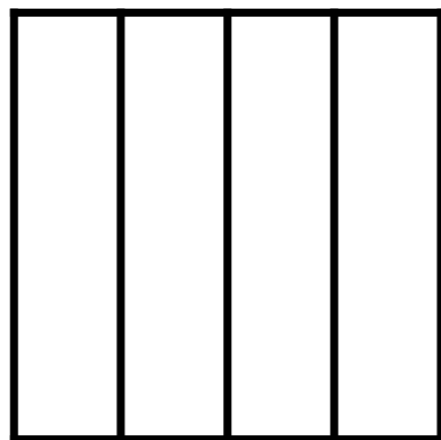
Representation of
rows of M in new
feature space

on

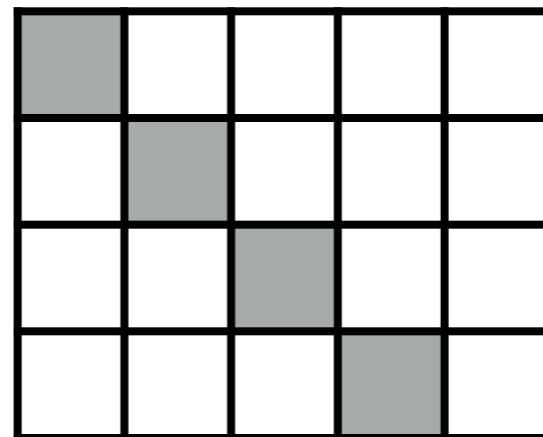
Principle
Components
(new features)



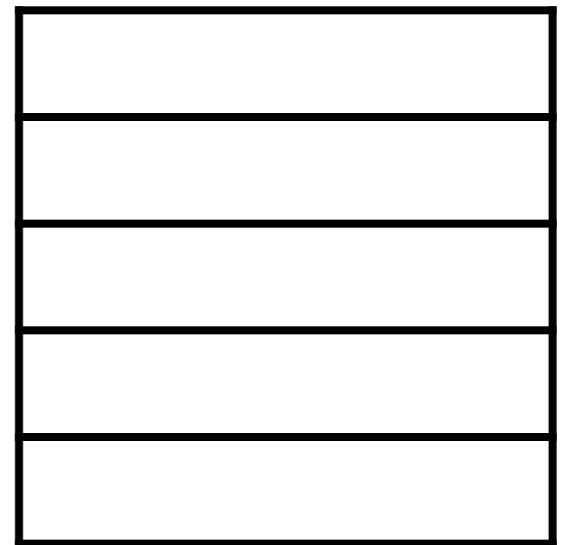
=



x



x



M

$m \times n$

U

$m \times m$

D

$m \times n$

V

$n \times n$

Data Matrix

Singular
Values of M

(#non-zero = rank M)

Singular Value Decomposition (SVD)

	the	congr ess	parlia ment	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Principal Value Position (SVD)

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Principal Value Position (SVD)

doc1 in old feature space

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

	3.06	0.00	0.00	0.00	0.00
	0.00	1.81	0.00	0.00	0.00
	0.00	0.00	0.57	0.00	0.00
	0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
	-0.65	-0.34	-0.51	-0.34	-0.31
	0.02	-0.54	0.34	-0.54	0.56
	-0.42	0.02	0.79	0.02	-0.44
	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Popular Value position (SVD)

doc1 in new feature space

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Principal Value Position (SVD)

*weight of component 1 for
doc 1*

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Principal Value Position (SVD)

*weight of component 1 over
all the data*

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Principal Value Position (SVD)

component 1

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

Popular Value position (SVD)

contribution of "the" to
component 1

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

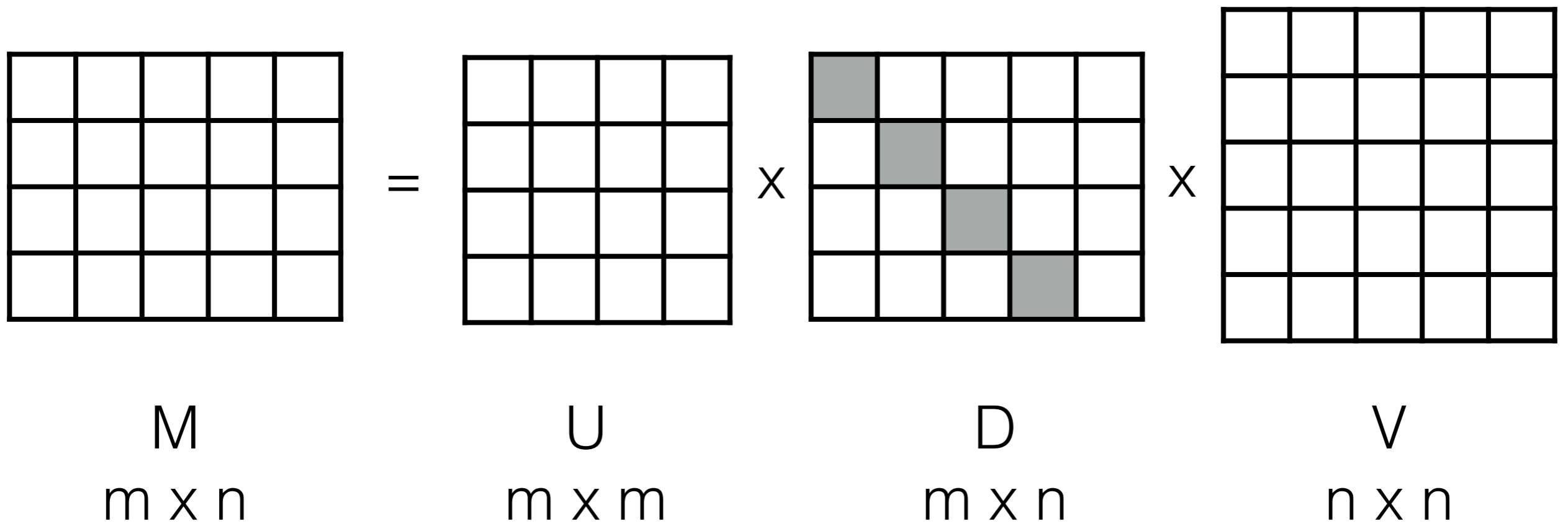
	3.06	0.00	0.00	0.00	0.00
	0.00	1.81	0.00	0.00	0.00
	0.00	0.00	0.57	0.00	0.00
	0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
	-0.65	-0.34	-0.51	-0.34	-0.31
	0.02	-0.54	0.34	-0.54	0.56
	-0.42	0.02	0.79	0.02	-0.44
	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

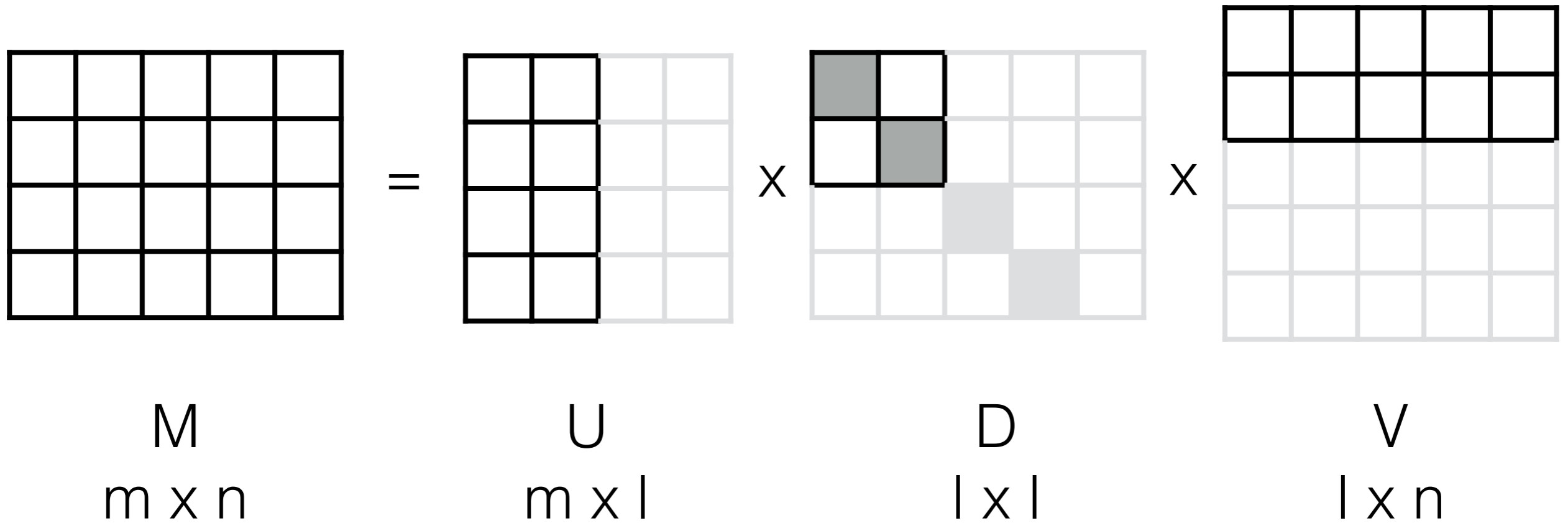
Singular Value Decomposition (SVD)





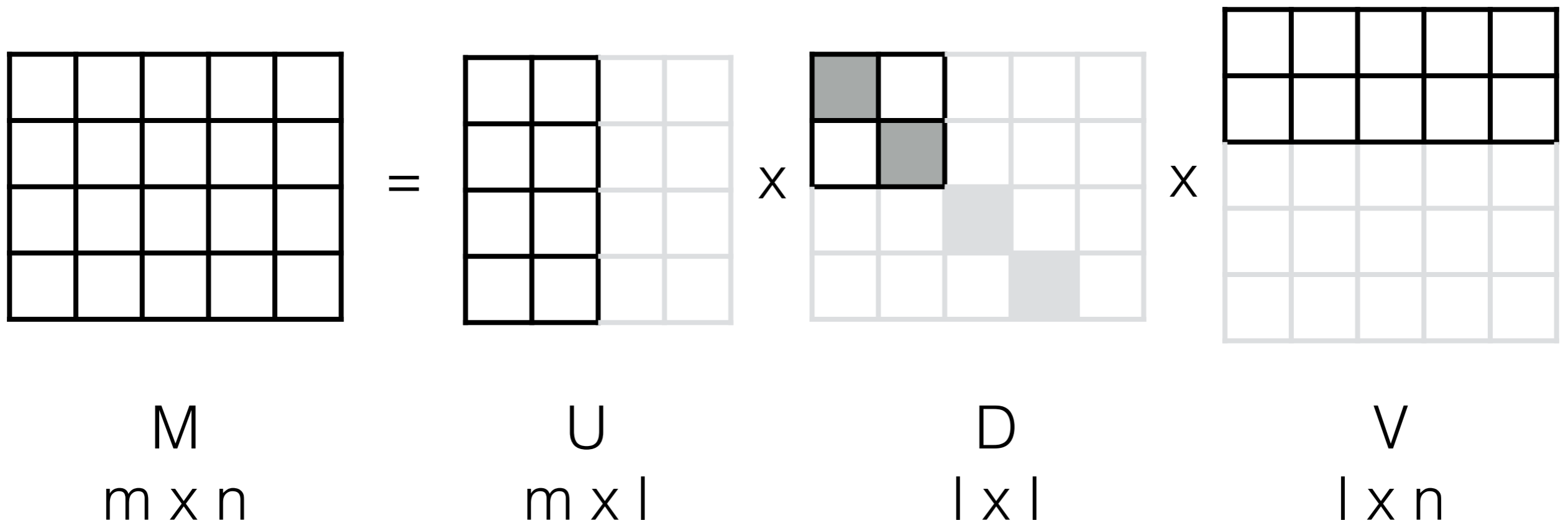
Truncated

Singular Value Decomposition (SVD)



Truncated

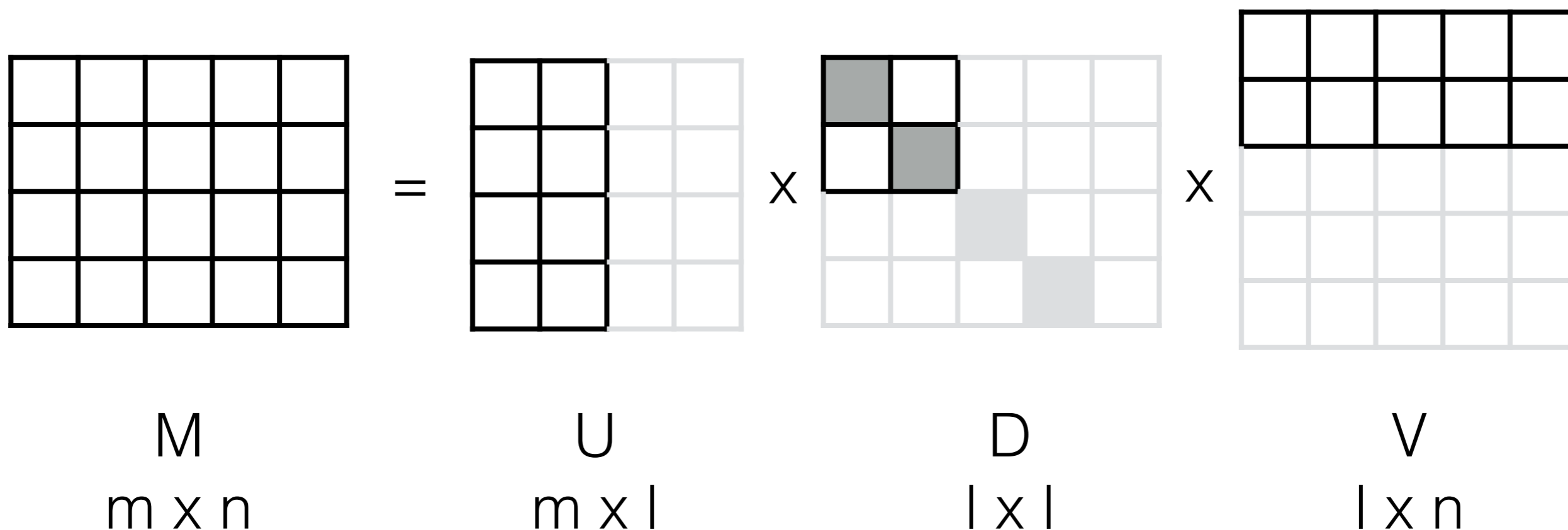
Singular Value Decomposition (SVD)



keep only first l components

Truncated

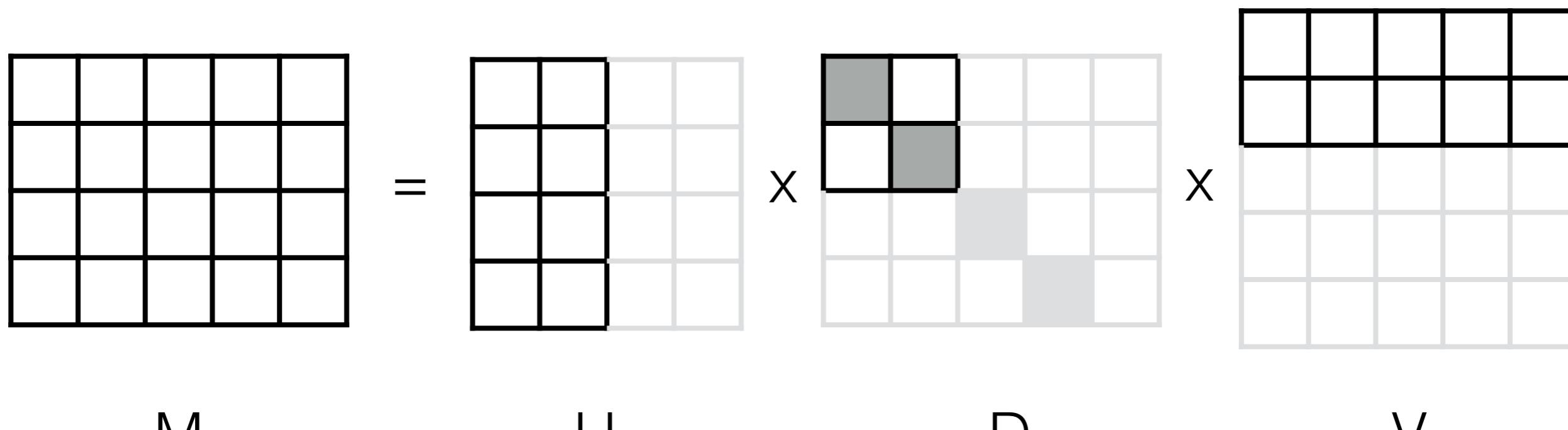
Singular Value Decomposition (SVD)



keep only first l components
"best l -rank approximation of M "

Truncated

Singular Value Decomposition (SVD)



M
 $m \times n$

$\|M - UDV\|^2$ as small as possible

keep only first L components
"best L -rank approximation of M "



Dimensionality Reduction

- “Low Rank Assumption”: we typically assume that our features contain a large amount of redundant information
- We can throw away a lot of principle components without losing too much of the signal needed for our task

Clicker Question!

Clicker Question!

In practice, is this assumption of low rank valid?

- a) Yes
- b) No
- c) Yeah, sure, why not?

Matrices IRL

Matrices IRL

- Data is noisy, so M is most likely full-rank

Matrices IRL

- Data is noisy, so M is most likely full-rank
- We assume that M is *close to* a low rank matrix, and we approximate the matrix it is close to

Matrices IRL

- Data is noisy, so M is most likely full-rank
- We assume that M is *close to* a low rank matrix, and we approximate the matrix it is close to
- Viewed as a “de-noised” version of M

Matrices IRL

- Data is noisy, so M is most likely full-rank
- We assume that M is *close to* a low rank matrix, and we approximate the matrix it is close to
- Viewed as a “de-noised” version of M
- “Original matrix exhibits redundancy and noise, low-rank reconstruction exploits the former to remove the latter”*

Matrices IRL

Matrices IRL

- Data is also often incomplete...missing values, new observations, etc.

Matrices IRL

- Data is also often incomplete...missing values, new observations, etc.
- Can we use SVD for this?

Matrices IRL

- Data is also often incomplete...missing values, new observations, etc.
- Can we use SVD for this?
- Yes! Though we need to make a few changes...

Matrix Completion

	roma	ballad of buster scruggs...	mud- bound	to all the boys i loved before	okja
user1	1	0	1		
user2	0			0	1
user3	1	0		1	0
user4		1	0		
user5					1

Matrix Completion

	roma	ballad of buster scruggs...	mud- bound	to all the boys i loved before	okja
user1	1	0	1	1	0
user2	0			0	1
user3	1	0	1	1	0
user4		1	0		
user5					1

"people also liked..."

Netflix Prize



[Home](#) |
 [Rules](#) |
 [Leaderboard](#) |
 [Update](#)

Leaderboard

Showing Test Score. [Click here to show quiz score](#)

Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos				
1	BellKor's Pragmatic Chaos	0.8567	10.06	2009-07-26 18:18:28
2	The Ensemble	0.8567	10.06	2009-07-26 18:38:22
3	Grand Prize Team	0.8582	9.90	2009-07-10 21:24:40
4	Opera Solutions and Vandelay United	0.8588	9.84	2009-07-10 01:12:31
5	Vandelay Industries !	0.8591	9.81	2009-07-10 00:32:20
6	PragmaticTheory	0.8594	9.77	2009-06-24 12:06:56
7	BellKor in BigChaos	0.8601	9.70	2009-05-13 08:14:09
8	Dace	0.8612	9.59	2009-07-24 17:18:43
9	Feeds2	0.8622	9.48	2009-07-12 13:11:51
10	BigChaos	0.8623	9.47	2009-04-07 12:33:59
11	Opera Solutions	0.8623	9.47	2009-07-24 00:34:07
12	BellKor	0.8624	9.46	2009-07-26 17:10:11

Matrix Completion

$$M \approx UDV = M'$$

Matrix Completion

$$\boxed{M} \approx UDV = \boxed{M'}$$

original completed

The diagram illustrates the matrix completion process. It shows the equation $\boxed{M} \approx UDV = \boxed{M'}$. The matrix M on the left is highlighted with a light blue background and is labeled 'original' below it with an upward-pointing arrow. The matrix M' on the right is also highlighted with a light blue background and is labeled 'completed' below it with an upward-pointing arrow. The expression UDV is positioned between the two matrices, with an approximation symbol \approx between M and UDV , and an equals sign $=$ between UDV and M' .

Matrix Completion

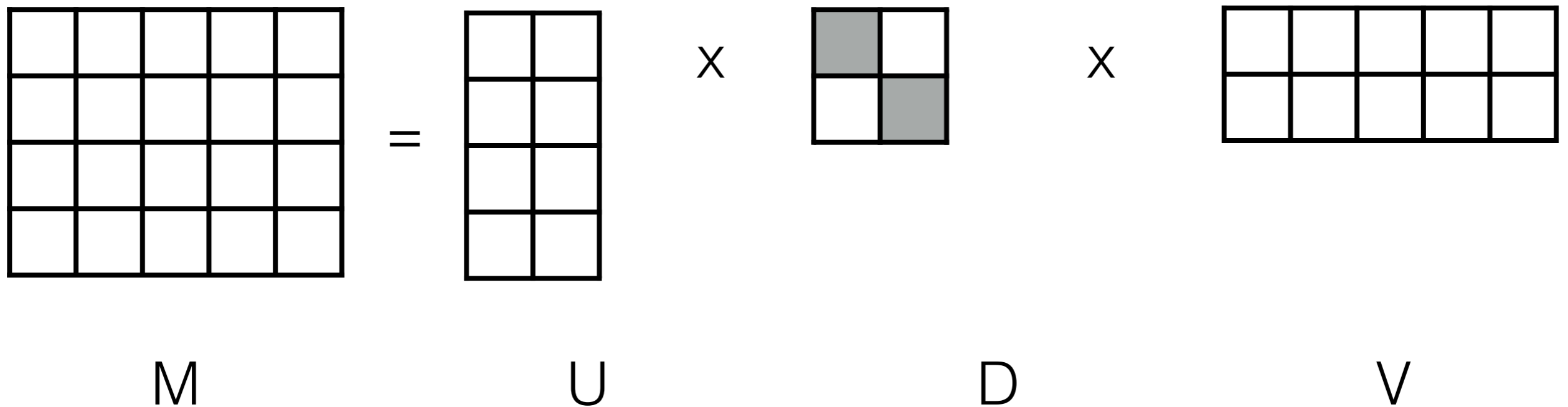
$$\mathbf{M} \approx \mathbf{UDV} = \mathbf{M}'$$

original

completed

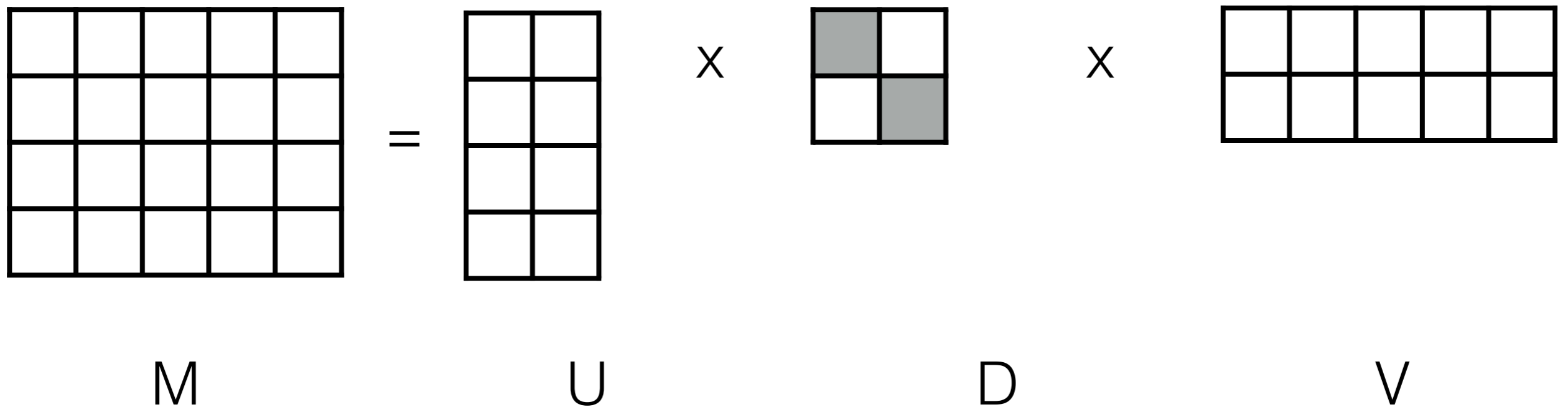
problems?

Matrix Completion



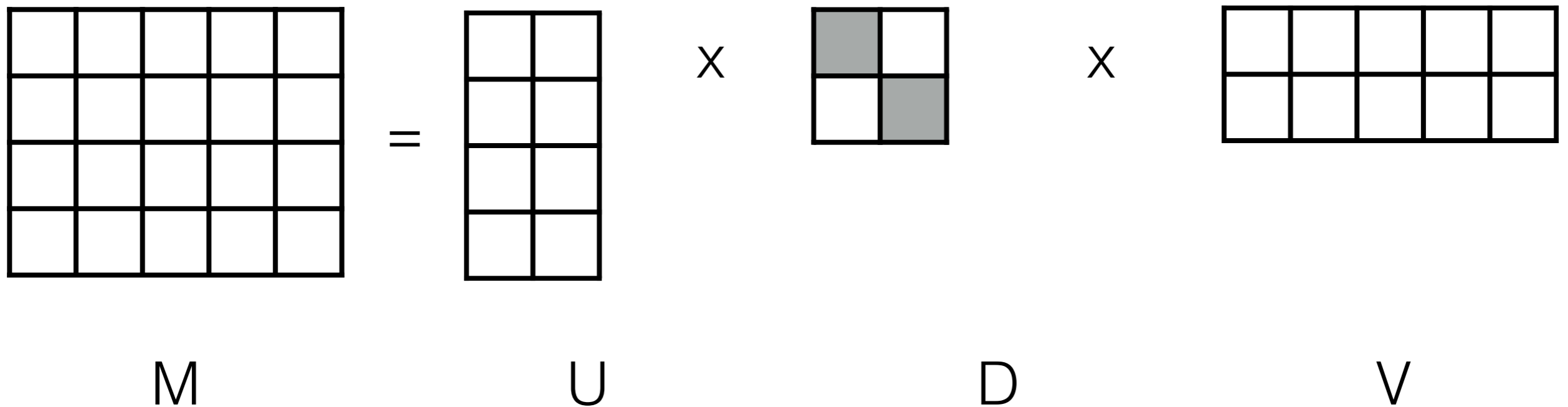
Exact SVD assumes M is complete...

Matrix Completion

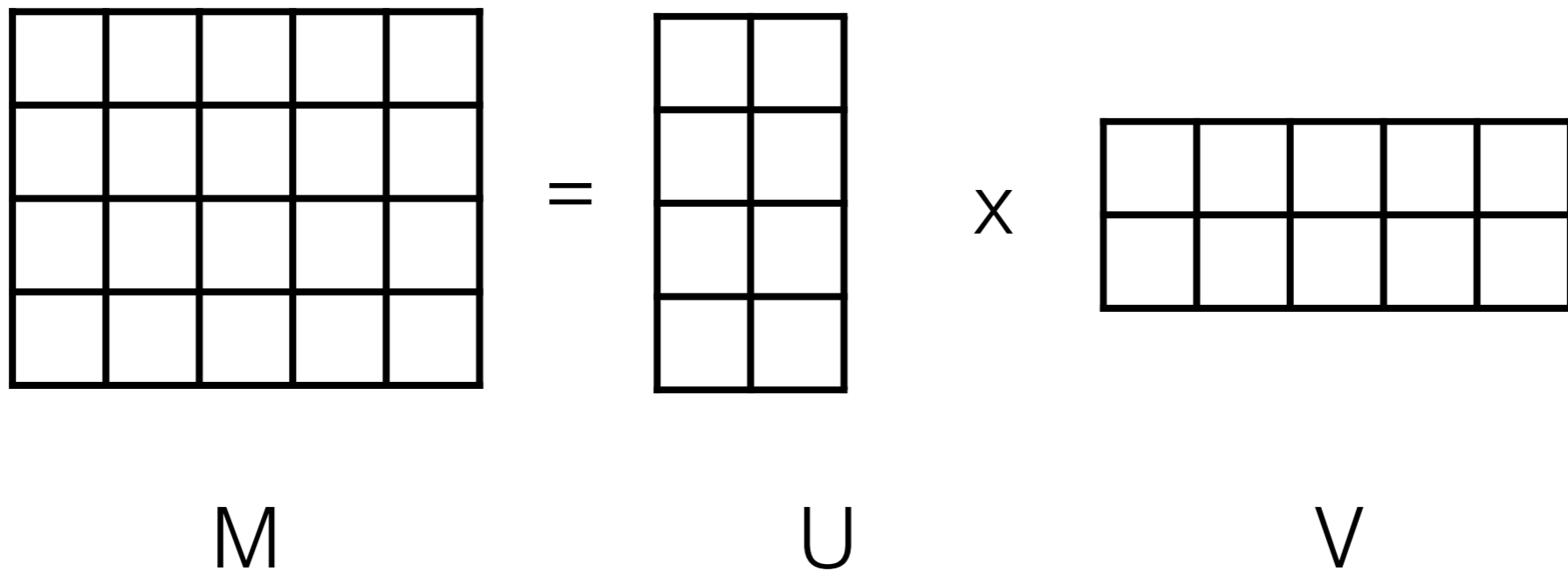


...just gradient descent that MF!

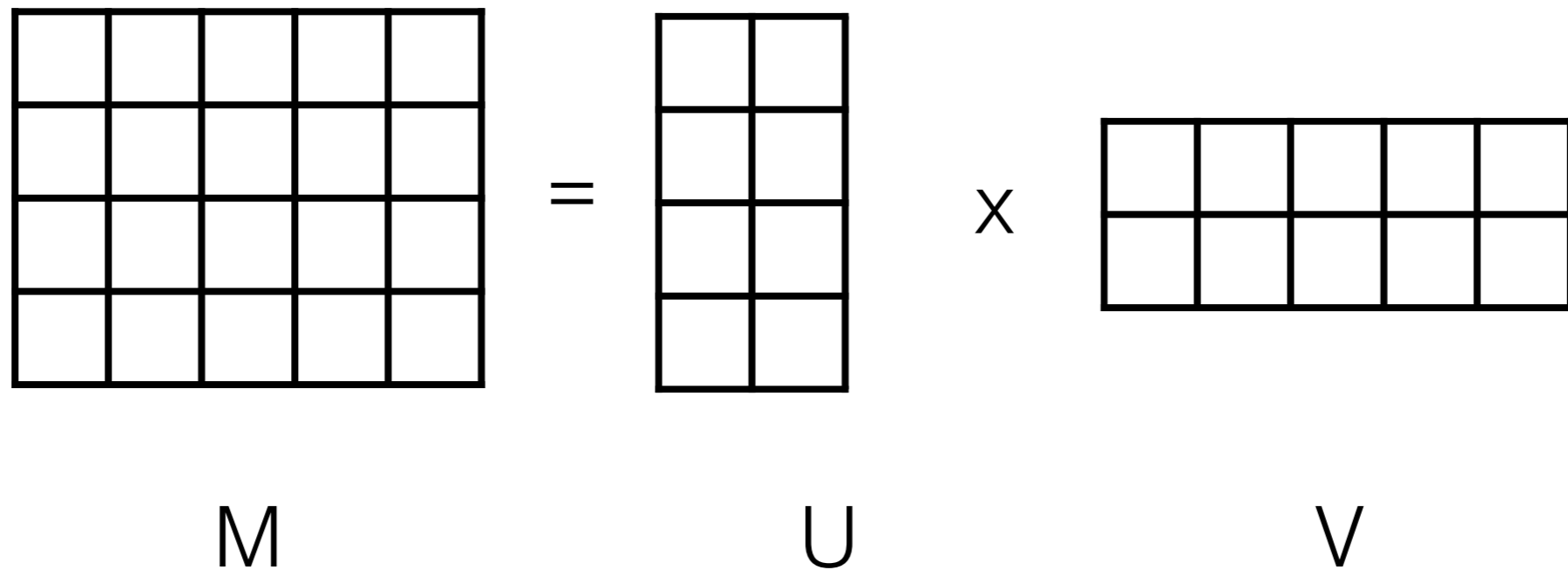
MF with Gradient Descent



MF with Gradient Descent

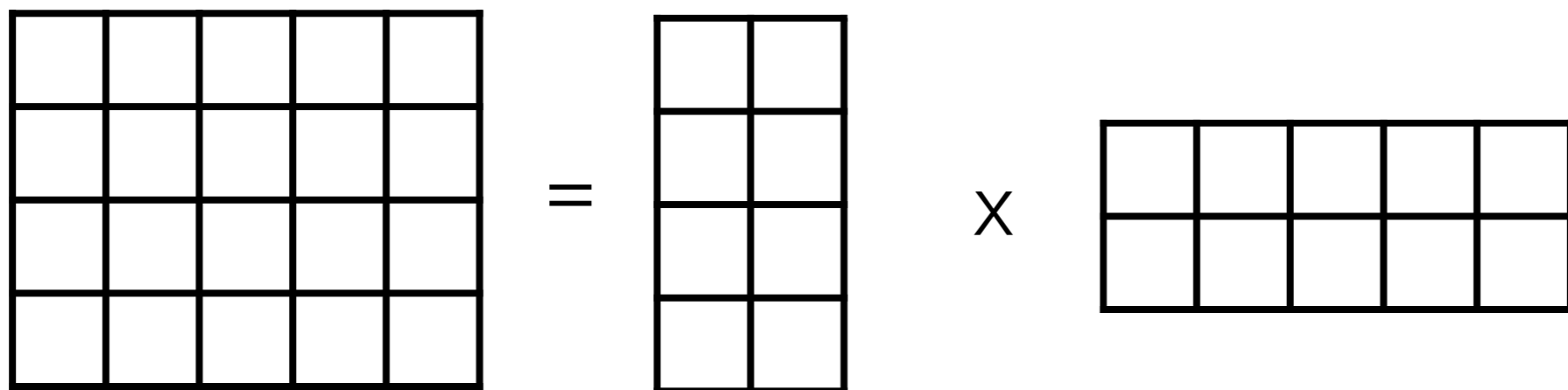


MF with Gradient Descent



Not properly SVD
(fewer guarantees, e.g. components not
orthonormal) but good enough

MF with Gradient Descent



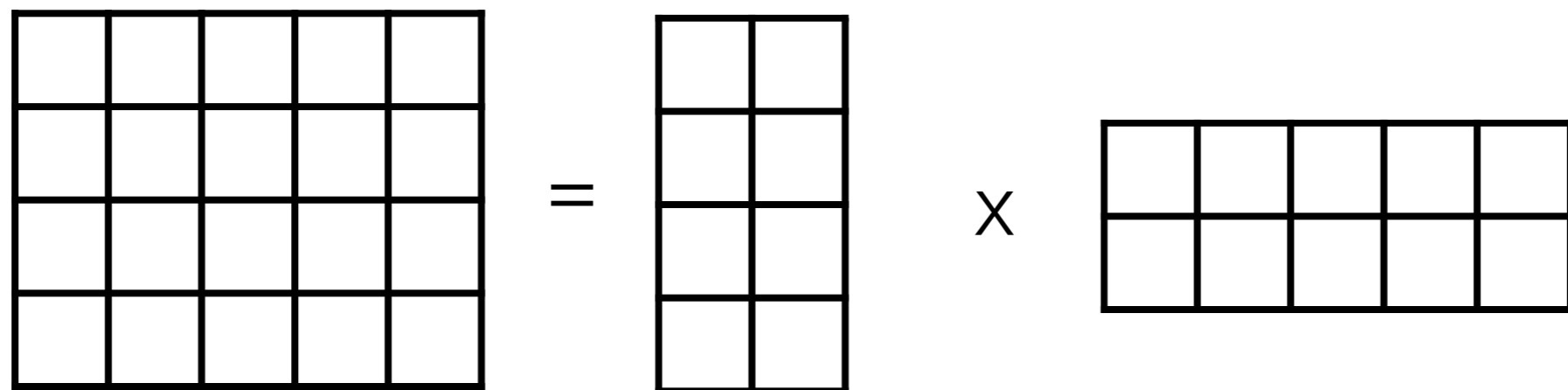
M

U

V

$$\min_{U, V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

MF with Gradient Descent



M

U

V

$$\min_{U, V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

But! Only consider cases when M_{ij} is observed!

Clicker Question!

Clicker Question!

$$\min_{U,V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

Compute the loss given this setting of U and V...

2	
	3
2	0

M

1
2
0

U

1	2
---	---

V

a) 14

b) 10

c) 6

Clicker Question!

$$\min_{U,V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

Compute the loss given this setting of U and V...

2	
	3
2	0

M

1
2
0

U

x

1	2
---	---

V

=

1	2
2	4
0	0

M'

a) 14

b) 10

c) 6

Clicker Question!

$$\min_{U,V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

Compute the loss given this setting of U and V...

2	
	3
2	0

M

1
2
0

U

x

1	2
---	---

V

=

1	2
2	4
0	0

M'

a) 14

b) 10

c) 6

Clicker Question!

$$\min_{U,V} \sum_{ij} (M_{ij} - u_i \cdot v_j)^2$$

Compute the loss given this setting of U and V...

2	
	3
2	0

M

1
2
0

U

x

1	2
---	---

$1 + 1 + 4$

V

=

1	2
2	4
0	0

M'

a) 14

b) 10

c) 6



Topic Models

Can you elaborate on exactly what the directions are in part 2 step 3, the stencil code does not quite imply what we are supposed to do...

When I try to display dots from part 2 on my mac (tried chrome, firefox, and safari), the elements do not appear in the html.

Changes I make to the nations.js file do not affect any of the html in after I load the nations.html file

Topic Models

Can you elaborate on exactly what the directions are in part 2 step 3, the stencil code does not quite imply what we are supposed to do...

When I try to display dots from part 2 on my mac (tried chrome, firefox, and safari), the elements do not appear in the html.

Changes I make to the nations.js file do not affect any of the html in after I load the nations.html file

instructions: stencil, instructions, part, step, rubric, handin...

UI: html, javascript, debug, display, elements...

systems: mac, windows, linux, chrome, firefox, os...

fillers: I, you, when, the, and, a

Topic Models

“Latent Semantic Analysis” (LSA)

$$P(w_i) = \sum_{j=1}^T P(w_i | z_i = j) P(z_i = j)$$

Topic Models

“Latent Semantic Analysis” (LSA)

$$P(w_i) = \sum_{j=1}^T P(w_i | z_i = j) P(z_i = j)$$

words are determined by topic
(and are conditionally independent of each other)

Topic Models

“Latent Semantic Analysis” (LSA)

$$P(w_i) = \sum_{j=1}^T P(w_i | z_i = j) P(z_i = j)$$

documents are a distribution over topics

C Models

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

C Models

component = "topic"

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

the	cong ress	parlia ment	US	UK
-0.65	-0.34	-0.51	-0.34	-0.31
0.02	-0.54	0.34	-0.54	0.56
-0.42	0.02	0.79	0.02	-0.44
-0.63	0.27	0.00	0.37	0.63
-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

C Models

component = "topic" =
distribution over words

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

	the	cong ress	parli ame	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

C Models

document = distribution
over topics

d1	-0.60	-0.39	0.70	0.00
d2	-0.48	0.50	-0.12	-0.71
d3	-0.43	-0.58	-0.69	0.00
d4	-0.48	0.50	-0.12	0.71

U

3.06	0.00	0.00	0.00	0.00
0.00	1.81	0.00	0.00	0.00
0.00	0.00	0.57	0.00	0.00
0.00	0.00	0.00	0.00	0.00

D

	the	cong ress	parlia ment	US	UK
d1	-0.65	-0.34	-0.51	-0.34	-0.31
d2	0.02	-0.54	0.34	-0.54	0.56
d3	-0.42	0.02	0.79	0.02	-0.44
d4	-0.63	0.27	0.00	0.37	0.63
	-0.04	0.73	0.00	-0.68	0.04

V

Topic Models

Factorization of the term-document matrix

	the	congress	parliament	US	UK
doc1	1	1	1	1	0
doc2	1	0	1	0	1
doc3	1	1	0	1	0
doc4	1	0	1	0	1

More on Thursday!

Word Embeddings

Factorization of the term-context matrix

	the	congress	parliament	US	UK
the	1	1	1	1	1
congress	1	1	0	1	0
parlaiment	1	0	1	1	1
US	1	1	1	1	0
UK	1	0	1	0	1

More on Thursday!

Word Embeddings

the con- parlia- US UK
gress ment

the	1	1	1	1	1
congress	1	1	0	1	0
parliament	1	0	1	1	1
US	1	1	1	1	0
UK	1	0	1	0	1

Embeddings!

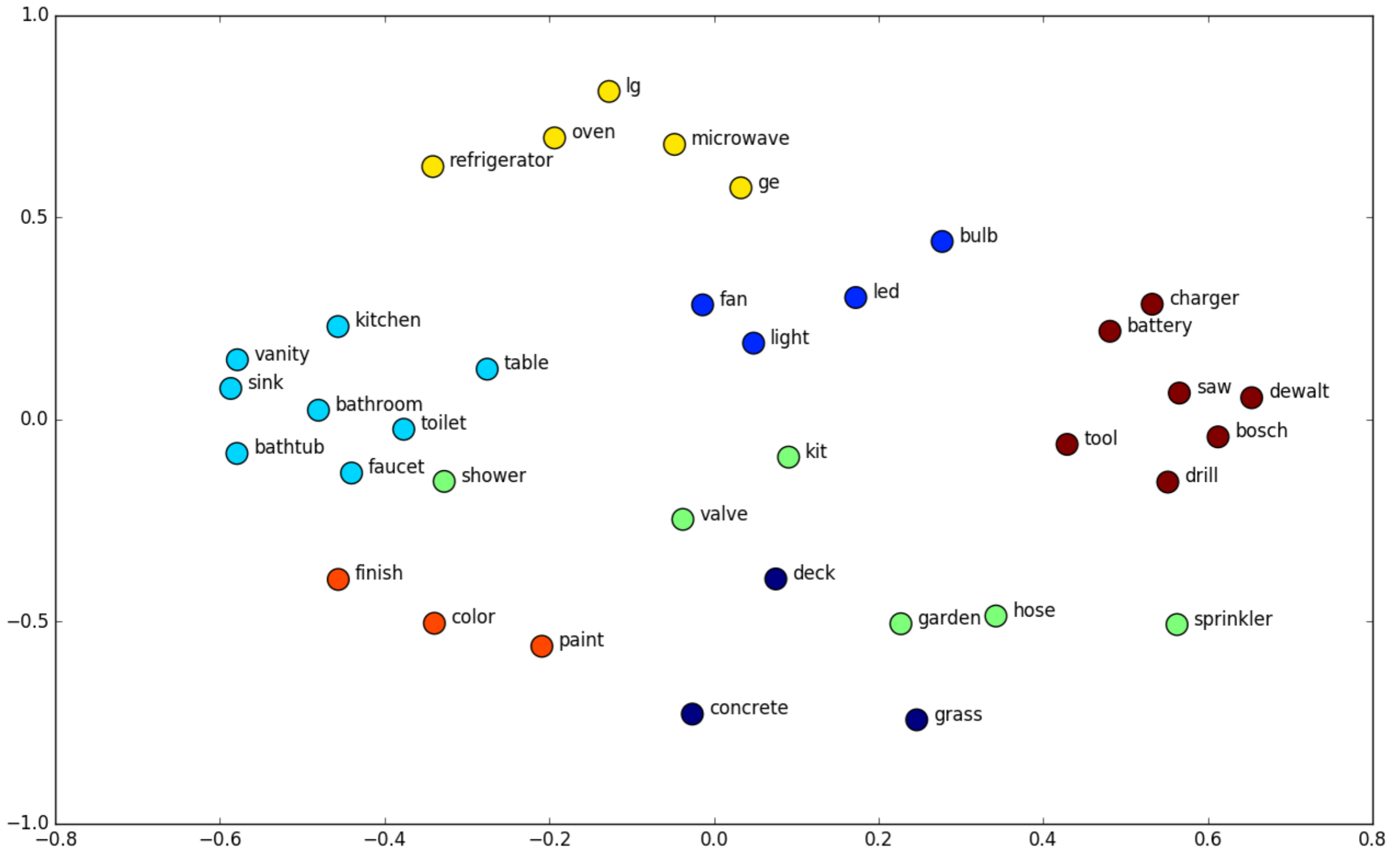
=

the	-0.60	-0.39	0.70	0.00
congress	-0.48	0.50	-0.12	-0.71
parliament	-0.43	-0.58	-0.69	0.00
US	-0.48	0.50	-0.12	0.71
UK	0.02	0.79	0.02	-0.44

-0.65	-0.34	-0.51	-0.34	-0.31
0.02	-0.54	0.34	-0.54	0.56
-0.42	0.02	0.79	0.02	-0.44
-0.63	0.27	0.00	0.37	0.63
-0.04	0.73	0.00	-0.68	0.04

More on Thursday!

Word Embeddings



Useful Resources/ References

- <https://github.com/uclmr/acl2015tutorial/>
- <https://web.stanford.edu/~jurafsky/li15/lec3.vector.pdf>
- <https://arxiv.org/pdf/1404.1100.pdf>
- <https://towardsdatascience.com/pca-and-svd-explained-with-numpy-5d13b0d2a4d8>
- http://nicolas-hug.com/blog/matrix_facto_3
- <https://machinelearningmastery.com/singular-value-decomposition-for-machine-learning/>
- <http://cocosci.princeton.edu/tom/papers/SteinversGriffiths.pdf>